## Dynamics of Uniform Circular Motion

1. Since an object in uniform circular motion is constantly accelerating there must be net force acting on the object.

$$
\Sigma \mathbf{F}_{\mathrm{r}}=\mathbf{m a} \mathbf{a}_{\mathrm{r}}=\mathbf{m v}^{2} / \mathbf{r}
$$

2. This net force is directed to the centre of the circular path and is known as the centripetal force (centre seeking).

3. There is no centrifugal force. The force you feel on the string is the reaction force of the ball. You pull on the ball to keep it changing direction and the ball pulls on you as a reaction force.
4. Forces on a tetherball see overhead.

Example 5-5 page 118: A 0.150 kg ball on the end of a 1.10 m long string is swung in a vertical circle. Determine the minimum speed the ball must have in order to continue to move in a circle. Calculate the tension in the string at the bottom of the circle assuming the ball is moving at twice the minimum speed of at the top.
Part 1:

$$
\begin{gathered}
\boldsymbol{\Sigma} \mathbf{F}_{\mathbf{r}}=\mathbf{m} \mathbf{v}^{2} / \mathbf{r} \\
\boldsymbol{\Sigma \mathbf { F } _ { \mathrm { r } } =} \mathrm{F}_{\mathrm{ta}}+\mathrm{mg}=\mathrm{mv}_{\mathrm{a}}^{2} / \mathrm{r}
\end{gathered}
$$

For the minimum speed $F_{t a}$ is zero so

$$
\begin{gathered}
\mathrm{mg}=\mathrm{mv}_{\mathrm{a}}^{2} / \mathrm{r} \\
\mathrm{v}_{\mathrm{a}}=\sqrt{\mathrm{gr}} \\
9.8 \mathrm{~m} / \mathrm{s}^{2} \times 1.10 \mathrm{~m}=3.28 \mathrm{~m} / \mathrm{s}
\end{gathered}
$$

## Part 2:

$$
\begin{gathered}
\mathrm{F}_{\mathrm{tb}}-\mathrm{mg}=\mathrm{mv}_{\mathrm{b}}^{2} / \mathrm{r} \\
\mathrm{~F}_{\mathrm{tb}}=\mathrm{mv}_{\mathrm{b}}^{2} / \mathrm{r}+\mathrm{mg} \\
\mathbf{F}_{\mathrm{tb}}=(\mathbf{0 . 1 5 0} \mathbf{k g}) \frac{(\mathbf{6 . 5 6 m} / \mathbf{s})^{2}}{(\mathbf{1 . 1 0 \mathrm { m } )}}+(\mathbf{0 . 1 5 0} \mathbf{k g})\left(\mathbf{9 . 8 0 \mathrm { m }} / \mathrm{s}^{\mathbf{2}}\right)=\mathbf{7 . 3 4 \mathrm { N }}
\end{gathered}
$$

