

## Translating English into Math

English	Math
7 more than a number $x$	$7 + x$ or $x + 7$
Twice a number	$2x$
4 less than a number	$x - 4$
3 more than one-half a number	$\frac{1}{2}x + 3$
John's age in 5 years, if John is $j$ years now	$j + 5$
Rachel's age last year if she is $r$ years now	$r - 1$
If the width is $w$ , find the length if the length is 4 more than twice the width	$l = 2w + 4$
If the length is $L$ , find the width if the width is 5 less than the length	$w = l - 5$

Let Statement

- ① {
  - ✓ Sketch a diagram or create a chart
  - ✓ Identify the UNKNOWN or UNKNOWNs, for example Mary's age now or the width
- ② ✓ Create an equation that describes the story
- ③ ✓ Solve the equation
- ④ ✓ Answer the question in a sentence

EXAMPLES

Jesse is 1 year older than three times as old as Ryan. In 6 years, the sum of their ages will be 61. How old are they now?

$$\begin{aligned} \text{Jesse} + \text{Ryan} &= 61 \\ (3r+7) + (r+6) &= 61 \\ 3r+7+r+6 &= 61 \\ 3r+r+7+6 &= 61 \\ \hline 4r+13 &= 61 \end{aligned}$$

$$\begin{aligned} 4r &= 48 \\ \frac{4r}{4} &= \frac{48}{4} \end{aligned}$$

$$r = 12$$

$$\begin{aligned} \text{Jesse} &= 3(12)+1 \\ &= 37 \end{aligned}$$

- Ryan is 12
- Jesse is 37

	Now	In 6 years
Jesse	$3r+1$	$(3r+1)+6 = 3r+7$
Ryan	$r=12$	$r+6$
Total		61

A number is doubled, and then decreased by 5. If the result is 9, find the original number.

• Let  $x$  be the number

$$\begin{aligned} 2x - 5 &= 9 \\ +5 \quad +5 \end{aligned}$$

$$\begin{aligned} 2x &= 14 \\ \frac{2x}{2} &= \frac{14}{2} \end{aligned}$$

$$x = 7$$

The number is 7

The perimeter of a rectangle is 46 cm. If the length is 5 cm less than three times the width. What are the dimensions

$$\begin{aligned} 3w - 5 \\ \hline \text{rectangle} \quad w = 7 \\ \hline 3(7) - 5 \\ 21 - 5 \end{aligned}$$

$$l = 16$$

The dimensions are 16 by 7

$$\text{FORMULA: } 2l + 2w = P$$

$$2(3w-5) + 2(w) = 46$$

$$6w - 10 + 2w = 46$$

$$\begin{aligned} 8w - 10 &= 46 \\ +10 \quad +10 \end{aligned}$$

$$\begin{aligned} 8w &= 56 \\ \frac{8w}{8} &= \frac{56}{8} \end{aligned}$$

$$w = 7$$

1. John is three times as old as Amy now. In 4 years the sum of their ages will be 36, find their ages now.

$$\begin{aligned}(3a+4) + (a+4) &= 36 \\ 3a+4 + a+4 &= 36 \\ 4a+8 &= 36 \\ 4a &= 28 \\ \boxed{a=7}\end{aligned}$$

	Now	In 4 years
John	$3a = 21$	$3a+4$
Amy	$a = 7$	$a+4$
Total		36

John is 21, Amy is 7

2. Paul is 11 years older than Rennie now. In 5 years the sum of their ages will be 23. Find their ages today.

$$\begin{aligned}(r+16) + (r+5) &= 23 \\ 2r + 21 &= 23 \\ 2r &= 2 \\ r &= 1\end{aligned}$$

	Now	In 5 years
Paul	$r+11=12$	$r+5+11 = r+16$
Rennie	$r = 1$	$r+5$
Total		23

Rennie is 1, Paul is 12

3. A number is tripled, and then decreased by 7. The result is <sup>32</sup>31. What is the number? **Let x be the number**

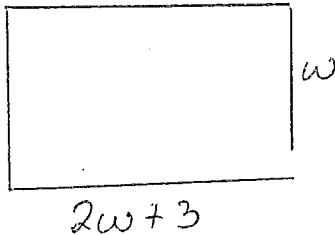
$$\begin{aligned}3x - 7 &= 32 \\ 3x &= 39 \\ x &= 13\end{aligned}$$

A is 13

4. A number is added to three times itself. Then, then decreased by 6. The result is 38. What is the number? **Let  $x$  be the number**

$$\begin{aligned}x + 3x - 6 &= 38 \\4x - 6 &= 38 \\4x &= 44 \\x &= 11\end{aligned}$$

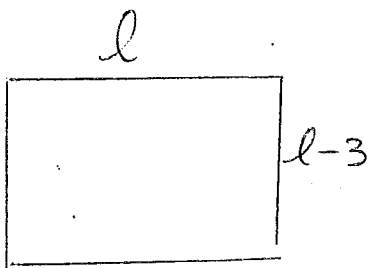
5. A rectangle has a perimeter of 60 cm. The length is 3 cm more than twice the width. What are the dimensions? **Sketch and label a diagram.**  
**Let  $w$  = the width**



$$\begin{aligned}2l + 2w &= P \\2(2w+3) + 2w &= 60 \\4w + 6 + 2w &= 60 \\6w + 6 &= 60 \\6w &= 54 \\w &= 9 \\l &= 21\end{aligned}$$

The dimensions are  
21 by 9  
cm cm

6. The width of a rectangle is 3 less than the length. If the perimeter is 34 cm, what are the dimensions? **Sketch and label a diagram.**  
**Let  $l$  = the length**



$$\begin{aligned}2l + 2w &= P \\2l + 2(l-3) &= 34 \\2l + 2l - 6 &= 34 \\4l - 6 &= 34 \\4l &= 40 \\l &= 10\end{aligned}$$

10cm by 7cm

7. When 8 is added to three times a number, the result is 41. What is the number?

Let  $x$  be the number

$$\begin{aligned} 8 + 3x &= 41 \\ 3x &= 33 \\ x &= 11 \end{aligned}$$

$$x = 11$$

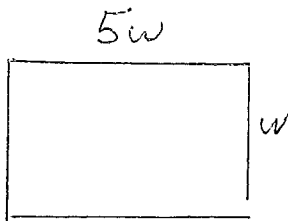
8. Next year, Paul will be twice as old as Francis. And the sum of their ages is 42. Find their ages today

$$\begin{aligned} 2(f+1) + f+1 &= 42 \\ 2f+2 + f+1 &= 42 \\ 3f + 3 &= 42 \\ 3f &= 39 \\ f &= 13 \end{aligned}$$

	Now	Next year
Paul	$2f+1$	$2(f+1)$ $2f+2$
Francis	$f=13$	$f+1$
Total		42

Francis is 13 and Paul is 27

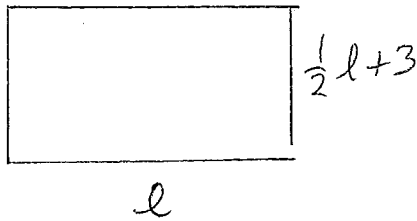
9. The perimeter of a rectangle is 126 cm. If the length is five times the width, find the dimensions of the rectangle. Let the width be  $w$



$$\begin{aligned} 2l + 2w &= P \\ 2(5w) + 2w &= P \\ 10w + 2w &= 126 \\ 12w &= 126 \\ w &= 10.5 \\ l &= 5(10.5) \\ &= 52.5 \end{aligned}$$

52.5 cm by 10.5 cm

10. The width of a rectangle is 3 cm more than one-half the length. If the perimeter is 54 cm, find the dimensions. **Let the length be L**



$$\begin{aligned}
 2l + 2w &= P \\
 2l + 2\left(\frac{1}{2}l + 3\right) &= 54 \\
 2l + l + 6 &= 54 \\
 3l + 6 &= 54 \\
 3l &= 48 \\
 l &= 16, \quad w = 11
 \end{aligned}$$

11. A number is doubled, and then increased by 5. That value is the same as the same number tripled then decreased by 2. What is the number?

**Let x be the number**

$$\begin{aligned}
 2x + 5 &= 3x - 2 \\
 7 &= x
 \end{aligned}$$

12. Teresa is 1 year older than twice Alex's age. In 7 years, the sum of their ages will be 52. How old are they now?

$$(2a + 8) + (a + 7) = 52$$

$$\begin{aligned}
 3a + 15 &= 52 \\
 3a &= 37 \\
 a &= 12.33
 \end{aligned}$$

$$\begin{aligned}
 \text{Alex is } &12 \\
 \text{Teresa is } &29
 \end{aligned}$$

	Now	In 7 years
Teresa	$2a + 8$	$2a + 15$
Alex	$a$	$a + 7$
Total		