

4.2 Adding Polynomials

MATHPOWER™ Nine, pp. 150-152

Green x^2 -tiles and x -tiles and red 1-tiles are positive. White algebra tiles are negative.

	Algebra Tile Representation	Algebraic Expression
		$x^2 + 2x + 2$
Add		$2x^2 + x + 1$
Result		$3x^2 + 3x + 3$

To add polynomials, collect like terms and add.

$$\begin{aligned} (x^2 + 3x - 3) + (2x^2 - x + 1) &= x^2 + 3x - 3 + 2x^2 - x + 1 \\ &= x^2 + 2x^2 + 3x - x - 3 + 1 \\ &= 3x^2 + 2x - 2 \end{aligned}$$

Model the expressions using algebra tiles or drawings on grid paper. Then, add.

1. $(x^2 + 2x + 2) + (2x^2 + x + 1)$

$$\begin{array}{r} \square\square\square + \square\square\square + \square\square\square \\ 3x^2 + 3x + 3 \end{array}$$

2. $\begin{array}{r} 2x^2 - x - 3 \\ + x^2 - x + 1 \\ \hline \end{array}$

$$3x^2 - 2x - 2$$

3. $(-2x^2 + 2x) + (-x^2 + x - 2)$

$$\begin{array}{r} -\square\square + \square\square + \square\square \\ -3x^2 + 3x - 2 \end{array}$$

4. $\begin{array}{r} x^2 - 3x + 2 \\ + (-2x^2) - x - 1 \\ \hline \end{array}$

$$-x^2 - 4x + 1$$

Simplify.

5. $(3y + 4z + 6) + (2y - z - 4)$

$$5y + 3z + 2$$

6. $2ab + 3bc + d + 2bc + 3ab - d$

$$5ab + 5bc$$

7. $x^2 - 2xy - y^2 + y^2 - 2xy + x^2$

$$2x^2 - 4xy$$

8. $s^2 + 4 + t + 3 + 2t^3 + 3s$

$$2t^3 + s^2 + 3s + t + 7$$

Add.

9. $4a + b$

$$+ 2a + 2b - 3$$

$$6a + 3b - 3$$

10. $4m^2 + 8mn + 2n^2$

$$+ m^2 - 2mn + n^2$$

$$5m^2 + 6mn + 3n^2$$

11. $3r^2 - 8r + 4$

$$+ r^2 - 2r + 5$$

$$4r^2 - 10r + 9$$

12. $c^2 + 2ac + 4$

$$+ 3c^2 + 6 + a^2$$

$$4c^2 + a^2 + 2ac + 10$$

Simplify.

13. $(4k^2 + 2k - 5) + (3 - k - 2k^2)$

$$2k^2 + k - 2$$

14. $(x^3 + 2y - 5) + (3x^3 - 4y + 7)$

$$4x^3 - 2y + 2$$

15. $(z^3x + 3z - 2) + (3z^3x - 4z + 6)$

$$4z^3x - 2z + 4$$