

## 1.1 ARITHMETIC SEQUENCES

The GENERAL TERM of an arithmetic sequence is

given by:

$$t_n = a + (n-1)d$$

$a$  = the 1st term

$n$  = the # of terms

$d$  = the common difference

$t_n$  = the general term / the last term

Arithmetic Sequences

3, 6, 9, 12, ... ✓

5, 10, 15, ... ✓

7, 5, 3, ... ✓

4, 5, 7, 10, ... ✗

Not arithmetic

2012-05-18

① Given 2, 5, 8, ... determine each term!

a)  $t_n$  (general term)

$$t_n = a + (n-1)d$$

$$a = 2$$

$$d = 3$$

$$t_n = 2 + (n-1)(3)$$

$$t_n = 2 + 3n - 3$$

$$t_n = 3n - 1$$

b)  $t_{80}$

" $a_{80}$ "

$$t_n = a + (n-1)d \quad \text{OR} \quad t_n = a + (n-1)d$$

$$t_{80} = 2 + (80-1)(3)$$

$$t_{80} = 3(80) - 1$$

$$t_{80} = 2 + (79)(3)$$

$$t_{80} = 240 - 1$$

$$t_{80} = 2 + 237$$

$$t_{80} = 239$$

$$t_{80} = 239$$

② Given 3, 5, 7, ... determine  $t_{75}$ .

$$a = 3$$

$$d = 2$$

$$n = 75$$

$$t_n = a + (n-1)d$$

$$t_{75} = 3 + (75-1)(2)$$

$$= 3 + (74)(2)$$

$$= 3 + 148$$

$$t_{75} = 151$$

③ Given 14, 25, 36... one term in the sequence is

234. Which term is it?  
 $14, 25, 36 \dots 234$   
 $1, 2, 3 \dots ?$

$$t_n = a + (n-1)d$$

$$234 = 14 + (n-1)(11)$$

$$\frac{220}{11} = \frac{(n-1)(11)}{11}$$

$$20 = n-1$$

$$\boxed{21 = n}$$

$$a = 14$$

$$d = 11$$

$$t_n = 234$$

④ Find the first term in an arithmetic sequence where the

5th term is 3 and the 25th term is -57.

$$t_5 = 3 \quad t_n = a + (n-1)d \quad t_{25} = -57$$

$$3 = a + 4d \quad \textcircled{1}$$

$$-57 = a + 24d \quad \textcircled{2}$$

$$\textcircled{1} - \textcircled{2} \quad \frac{60}{-20} = \frac{-20d}{-20}$$

$$\frac{60}{-20} = d$$

$$\underline{\underline{d = -3}}$$

sub into ①  $3 = a + 4(-3)$

$$3 = a - 12$$

$$\boxed{15 = a}$$

⑤ Find the first term in an arithmetic sequence where

$t_{50} = 152$  and  $t_{200} = 602$ .

$$152 = a + 49d \quad \textcircled{1}$$

$$-602 = a + 199d \quad \textcircled{2}$$

$$-450 = -150d$$

$$d = \frac{-450}{-150}$$

$$\underline{\underline{d = 3}}$$

sub into ①

$$152 = a + 49(3)$$

$$152 = a + 147$$

$$\boxed{a = 5}$$

⑥ Determine the first four terms in the sequence  $\left\{ \frac{n+3}{n^2+1} \right\}$

$$t_1 = \frac{1+3}{1^2+1} = \frac{4}{2} = 2$$

$$t_2 = \frac{2+3}{2^2+1} = \frac{5}{5} = 1$$

$$t_3 = \frac{3+3}{3^2+1} = \frac{6}{10} = \frac{3}{5}$$

$$t_4 = \frac{4+3}{4^2+1} = \frac{7}{17}$$

7) Determine the value of  $x$  and  $a$  such that the following is an arithmetic sequence: <sup>first term</sup>

$$x+2, 3x-1, 2x+1$$

2<sup>nd</sup> Term - 1<sup>st</sup> Term = 3<sup>rd</sup> Term - 2<sup>nd</sup> Term  
(both equal  $d$ )

$$3x-1-(x+2) = 2x+1-(3x-1)$$

$$3x-1-x-2 = 2x+1-3x+1$$

$$2x-3 = -x+2$$

$$3x = 5$$

$$\boxed{x = \frac{5}{3}}$$

$$\boxed{a = \frac{11}{3}}$$

Pg 9

$$\# 2 (a, e)$$

$$\# 8-11 (a, e)$$

$$\# 14$$

$$t_n = a + (n-1)d$$

$$2x+1 = x+2 + (2)(2x-3)$$

$$2x+1 = x+2+4x-6$$

$$2x+1 = 5x-4$$

$$5 = 3x$$

$$\frac{5}{3} = x$$

## 1.2 Arithmetic Series

NSB 1109 2012-05-18

Sequence: 3, 6, 9, ...

Series:  $3 + 6 + 9 + \dots$

The sum of the first  $n$  terms of the general arithmetic series is:

$$S_n = \frac{n}{2} (a + l)$$

OR

$$S_n = \frac{n}{2} (2a + (n-1)d)$$

$n$  = # of terms  
 $a$  = first term  
 $l$  = last term

$n$  = # of terms  
 $d$  = common difference  
 $a$  = 1<sup>st</sup> term

- ① Determine the sum of the first 50 terms of the arithmetic series  $3 + 4.5 + 6 + \dots$

$$n = 50$$

$$a = 3$$

$$d = 1.5$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{50} = \frac{50}{2} [6 + (49)(1.5)]$$

$$S_{50} = 25 [6 + 73.5] = \boxed{1987.5}$$

- ② Determine the sum given  $1 + 5 + 9 + \dots + 97$ .

$$a = 1$$

$$d = 4$$

$$t_n = l = 97$$

1. Determine  $n$

$$t_n = a + (n-1)d$$

$$97 = 1 + (n-1)4$$

$$96 = 4n - 4$$

$$100 = 4n$$

$$n = \underline{\underline{25}}$$

2. Determine sum

$$S_n = \frac{n}{2} (a + l)$$

$$S_{25} = \frac{25}{2} (1 + 97)$$

$$S_{25} = \boxed{1225}$$

- ③ Determine  $d$  if  $S_7 = 91$  and  $a = 19$ .

$$a = 19$$

$$n = 7$$

$$S_7 = 91$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$91 = 3.5 [38 + 6d]$$

$$\frac{91}{3.5} = 38 + 6d$$

$$26 = 38 + 6d$$

$$-12 = 6d$$

$$d = \boxed{-2}$$

④ Determine the sum of  $3 + 5 + 7 + \dots + (2n+1)$

$$a = 3$$

$$d = 2$$

$$l = 2n+1$$

$$n = n$$

$$S_n = \frac{n}{2} (a + l)$$

$$= \frac{n}{2} (3 + 2n+1)$$

$$= \frac{n}{2} (2n+4)$$

$$= \frac{2n^2 + 4n}{2} = \boxed{n^2 + 2n}$$

⑤ Find two arithmetic means between 17 and 59.

$$17, \text{---}, \text{---}, 59$$

$$t_4 = 59$$

$$a = 17$$

$$n = 4$$

$$t_n = a + (n-1)d$$

$$59 = 17 + (3)d$$

$$42 = 3d$$

$$d = 14$$

$$\text{Arithmetic Means: } 17 + 14 = \boxed{31} + 14 = \boxed{45}$$

⑤ In an ice cream store, the sale of ice cream increases by \$5 per week during a 15 week season.

Suppose the profit for the first week is \$30,

determine the profit for the entire season.

$$d = 5$$

$$n = 15$$

$$a = 30$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{15} = \frac{15}{2} [60 + (14)(5)]$$

$$S_{15} = 7.5 [60 + 70]$$

$$S_{15} = 7.5 [130]$$

$$S_{15} = \boxed{\$975.00}$$

B, 16

#1 (b, c, e)

#2, 4 (a, c, e)

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### 1.3 Geometric Sequences

2015-01-10

Sequences whose terms result from multiplying the previous term by a common ratio are called

GEOMETRIC SEQUENCES

$$t_n = ar^{n-1}$$

$a$  = 1st term

$r$  = common ratio

$n$  = # of terms

$t_n$  = general term / last term

Ex 2, 4, 8, 16, 32, 64...

$$r = \frac{4}{2} = \frac{8}{4} = \frac{t_{n+1}}{t_n}$$

① Given -999, -111,  $-\frac{37}{3}$  ... find  $t_6$

$$t_n = ar^{n-1}$$

$$t_6 = (-999)\left(\frac{1}{9}\right)^5$$

$$t_6 = (-999)\left(\frac{1}{59049}\right)$$

$$t_6 = \frac{-37}{2187} \text{ OR } -0.017$$

② Given  $t_4 = 3$  and  $t_8 = 243$  find  $t_{11}$  in a geometric sequence.

$$t_n = ar^{n-1}$$

$$3 = ar^3 \quad \textcircled{1}$$

$$243 = ar^7 \quad \textcircled{2}$$

$$\textcircled{2} \div \textcircled{1}$$

$$3 = a(\pm 3)^3$$

$$3 = a(\pm 27)$$

$$a = \frac{3}{\pm 27} \quad a = \pm \frac{1}{9}$$

$$81 = r^4$$

$$r = \pm 3$$

↑  
even exponent

$$t_{11} = \left(\pm \frac{1}{9}\right)(\pm 3)^{10}$$

$$t_{11} = \left(\pm \frac{1}{9}\right)(\pm 59049)$$

$$\therefore t_{11} = \pm 6561$$

③ Given  $t_3 = 59049$ ,  $t_6 = 81$  in a geometric sequence find  $t_{10}$ .

$$t_n = ar^{n-1}$$

$$59049 = ar^2 \quad ①$$

$$81 = ar^5 \quad ②$$

$$① \div ②$$

$$729 = r^{-3}$$

$$\frac{1}{729} = r^3$$

$$\frac{1}{9} = r$$

$$81 = a \left(\frac{1}{9}\right)^5$$

$$81 = a \left(\frac{1}{59049}\right)$$

$$a = 4782969$$

$$t_{10} = (4782969) \left(\frac{1}{9}\right)^9$$

$$t_{10} = \frac{1}{81} \text{ OR } 0.0123\ldots$$

④ If  $x-3$ ,  $x+1$ ,  $4x-2$  are consecutive terms of a geometric sequence, find  $x$

$$\frac{x+1}{x-3} = \frac{4x-2}{x+1}$$

$$\frac{2^{\text{nd}} \text{ term}}{1^{\text{st}} \text{ term}} = \frac{3^{\text{rd}} \text{ term}}{2^{\text{nd}} \text{ term}}$$

$$(4x-2)(x-3) = (x+1)(x+1)$$

$$4x^2 - 14x + 6 = x^2 + 2x + 1$$

$$3x^2 - 16x + 5 = 0$$

$$3x^2 - 15x - x + 5 = 0$$

$$3x(x-5) - 1(x-5) = 0$$

$$(3x-1)(x-5) = 0$$

$$x = \frac{1}{3} \quad x = 5$$

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\* 1, 2, 4 (a, ar, ar^2)

\* 7, 8

### 1.4 Geometric Series

Notes Title

2023-05-24

2+4+8+16+... is a geometric series

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_n = \frac{a-r \cdot l}{1-r}$$

\* Use if you know the last term

$l =$  last term

1) Determine  $S_8$ , if  $a=12$ ,  $t_5=192$  (geometric series)

$$t_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$192 = 12r^4$$

$$S_8 = \frac{12(1-(r^8))}{1-(r^2)}$$

$$16 = r^4$$

$$r = \pm 2$$

$$S_8 = \frac{12(1-256)}{1-(\pm 2)}$$

$$= \frac{-3060}{-1} \text{ OR } \frac{-3060}{3}$$

$$= 3060 \text{ OR } -1020$$

2) Determine the sum of each geometric series

a)  $\sum_{k=2}^9 18(0.1)^k$

$$a = 18(0.1)^2 = 0.18$$

$$n = 9 - 2 + 1$$

$$n = 8$$

$$\text{2nd term} = 18(0.1)^3 = 0.018$$

$$r = \frac{0.018}{0.18} = 0.1$$

$$l = 18(0.1)^9 \rightarrow 1.8(\text{EXP})^{-8}$$

$$l = 1.8 \times 10^{-8}$$

$$S_n = \frac{a-r \cdot l}{1-r}$$

$$S_8 = \frac{0.18 - (0.1)(1.8 \times 10^{-8})}{1 - 0.1}$$

$$= 0.20$$



$$b) \sum_{k=0}^9 \frac{3}{5^{k+1}}$$

$$a = \frac{3}{5} = 0.6$$

$$\text{2nd term: } \frac{3}{25} = 0.12$$

$$r = \frac{0.12}{0.6} = \frac{1}{5} = 0.2$$

$$n = 10$$

$$l = \frac{3}{5^{10}}$$

$$S_n = \frac{a - r \cdot l}{1 - r}$$

$$S_{10} = \frac{0.6 - (0.2) \left( \frac{3}{5^{10}} \right)}{1 - 0.2}$$

$$S_{10} = 0.75$$

3) Write the following using sigma notation

$$a) 8 + 4 + 2 + \dots + \frac{1}{64}$$

$$\sum_{k=1}^n ar^{k-1} \rightarrow \sum_{k=1}^n (8) \left( \frac{1}{2} \right)^{k-1}$$

$$l_n = ar^{n-1}$$

$$\frac{1}{64} = 8 \left( \frac{1}{2} \right)^{n-1}$$

$$\frac{1}{512} = \left( \frac{1}{2} \right)^{n-1}$$

$$\left( \frac{1}{2} \right)^9 = \left( \frac{1}{2} \right)^{n-1}$$

$$9 = n - 1$$

$$\underline{\underline{n = 10}}$$

$$\sum_{k=1}^{10} 8 \left( \frac{1}{2} \right)^{k-1}$$

$$b) -12 - 6 - 3 - \dots - \frac{3}{16}$$

$$\textcircled{1} \sum_{k=1}^n (-12) \left( \frac{1}{2} \right)^{k-1}$$

$$l_n = ar^{n-1}$$

$$-\frac{3}{16} = (-12) \left( \frac{1}{2} \right)^{n-1}$$

$$\frac{1}{64} = \left( \frac{1}{2} \right)^{n-1}$$

$$\left( \frac{1}{2} \right)^6 = \left( \frac{1}{2} \right)^{n-1}$$

$$\underline{\underline{n = 7}}$$

By 28  
\* 1, 3, 4 (a, s, e)  
5, 12

$$\sum_{k=1}^7 (-12) \left( \frac{1}{2} \right)^{k-1}$$

### 1.5 Infinite Geometric Series

The sum of an infinite geometric series where

$$-1 < r < 1 \text{ or } |r| < 1 \text{ is:}$$

↳ "Absolute Value"

$$S_{\infty} = \frac{a_1}{1-r}$$

on Formula Sheet  
(Series Converges / CONVERGENT)

\* If  $r$  is NOT between  $-1$  and  $1$ ,  
NO FINITE SUM (Diverges / DIVERGENT)

① Determine the sum where a sum to infinity exists:

a)  $15 - 9 + \frac{27}{5} - \dots$

$$r = -0.6$$

$$-1 < -0.6 < 1 \quad \checkmark \quad \text{CONVERGENT}$$

\* Find the sum

$$S = \frac{15}{1 - (-0.6)} = 9.375$$

② Determine the sum

a)  $\sum_{i=0}^{\infty} 2(0.9)^i$

$$a = 2(0.9)^0 = 2$$

$$\text{2nd term} = 2(0.9)^1 = 1.8$$

$$r = \frac{1.8}{2} = 0.9$$

$$S_{\infty} = \frac{2}{1 - 0.9}$$

$$S_{\infty} = 20$$

b)  $-4 + 6 - 9 + \dots$

$$r = \frac{6}{-4} = -1.5 \quad \times \quad \text{DIVERGENT}$$

NO FINITE SUM / DIVERGENT

$$b) \sum_{i=1}^{\infty} 3\left(\frac{7}{6}\right)^i$$

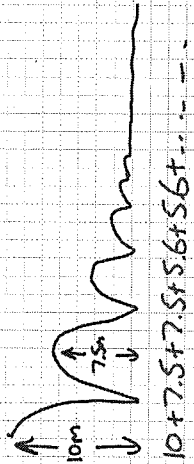
$$a = 3\left(\frac{7}{6}\right) = \frac{21}{6} = 3.5$$

$$\text{2nd term: } 3\left(\frac{7}{6}\right)^2 = 4.08\bar{3} \rightarrow \frac{2^{\text{nd}}}{1^{\text{st}}} = \frac{3\left(\frac{7}{6}\right)^2}{3\left(\frac{7}{6}\right)} = \frac{7}{6} \approx 1.1\bar{6}$$

NO FINITE SUM / DIVERGENT

3) A ball is dropped from a height of 10m. On each bounce the ball rises to 75% of the height from which it fell.

a) Find the total distance the ball travels before coming to rest.



Infinite Sums

$$S = 2\left(\frac{a}{1-r}\right) - a$$

\*NOT ON FORMULA SHEET

b) Find the vertical distance that the ball travels up to and including its 8th bounce

$$n = 8$$

$$a = 10$$

$$r = 0.75$$

$$S = 2\left(\frac{a(1-r^n)}{1-r}\right) - a$$

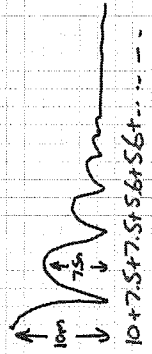
$$S_8 = 2\left(\frac{10(1-0.75^8)}{1-0.75}\right) - 10$$

$$S_8 = 61.99 \text{ m}$$

$$S = 2\left(\frac{10}{1-0.75}\right) - 10$$

$$S = 70 \text{ m}$$

c) How high did the ball bounce immediately after its 4th bounce?



$$t_n = ar^{n-1}$$

$$t_4 = 7.5(0.75)^3 \quad \text{OR} \quad t_5 = 10(0.75)^4$$

$$\text{OR } t_5 = 10(0.75)^4$$

Ry 35

# 1-3 (a, c, e)

S(a, b)

\* Review Questions

Ry 40

\* 1-53

(4) Find the rational number represented by the repeating decimal:

a)  $0.\overline{17}$

$$0.\overline{17} = \frac{1}{10} + \frac{7}{100} + \frac{7}{1000} + \frac{7}{10000} + \dots$$

$$r = \frac{1}{10}$$

$$S = \frac{a}{1-r} = \frac{1}{10} + \frac{\frac{7}{100}}{1 - \frac{1}{10}} = \frac{1}{10} + \frac{\frac{7}{100}}{\frac{9}{10}} = \frac{1}{10} + \frac{7}{100} \cdot \frac{10}{90} = \frac{1}{10} + \frac{7}{90}$$

$$= \frac{1}{10} + \frac{7}{90} = \frac{9}{90} + \frac{7}{90} = \frac{16}{90}$$

b)  $2.\overline{524}$

$$2.\overline{524} = 2 + \frac{5}{10} + \frac{24}{1000} + \frac{24}{100000} + \dots$$

$$r = \frac{1}{100}$$

$$= 2 + \frac{5}{10} + \frac{\frac{24}{1000}}{1 - \frac{1}{100}} = 2 + \frac{5}{10} + \frac{24}{1000} \cdot \frac{100}{99} = 2 + \frac{5}{10} + \frac{24}{990}$$

$$= 2 + \frac{5}{10} + \frac{24}{990} = 2 + \frac{495}{990} + \frac{24}{990} = 2 \frac{519}{990}$$

## SIGMA NOTATION

3012-05-23

$\sum$  "sigma" is used to represent a sum of terms

$$\sum_{k=1}^4 5k = 5(1) + 5(2) + 5(3) + 5(4)$$

$$= 5 + 10 + 15 + 20$$

$$= 50$$

Upper Limit

Lower Limit

① Write in expanded form + determine the sum

$$a) \sum_{k=3}^9 2k$$

$$= 6 + 8 + 10 + 12 + 14 + 16 + 18$$

$$= \boxed{84}$$

$$b) \sum_{k=-2}^3 k^2 + k$$

$$= (-2)^2 + (-2) + (-1)^2 + (-1) + 0^2 + 0 + 1^2 + 1 + 2^2 + 2 + 3^2 + 3$$

$$= 2 + 0 + 0 + 2 + 6 + 12$$

$$= \boxed{22}$$

\* If the summation expression is a linear function, then the summation is an arithmetic series

$$\text{Ex } \sum_{k=1}^{10} 3k + 2 \rightarrow \text{Arithmetic Series since } y = 3k + 2 \text{ is linear}$$

\* Can use arithmetic series formula

$$\sum_{k=1}^{10} 3k^2 + 2 \rightarrow \text{Not an Arithmetic Series since } y = 3k^2 + 2 \text{ is non-linear}$$

Upper Limit - Lower Limit + 1 = # of terms

$$\text{Ex } \sum_{k=3}^{11} 4k+1 \quad \# \text{ of terms: } |11-3+1| = 9 \text{ terms when expanded}$$

Linear  $\therefore$  use sum formula  $S_n = \frac{n}{2}(a+l)$

$$n = 50 \quad a = 4(1) - 1 \quad l = 4(50) - 1 \quad S_{50} = \frac{50}{2}(3+199)$$

$\uparrow$   $a = 3$   $l = 199$

$$50 - 1 + 1 \quad \boxed{S_{50} = 5050}$$

2) Evaluate (Determine the sum)

$$a) \sum_{k=1}^{50} 4k - 1$$

$$b) \sum_{k=4}^{35} 4-2k$$

$$a = -4$$

$$l = -66$$

$$n = 32$$

$$S_n = \frac{n}{2}(a+l)$$

$$S_{32} = \frac{32}{2}(-4+(-66))$$

$$\boxed{S_{32} = -1120}$$

3) Write the sum using sigma notation

$$a) \frac{1}{2} + \frac{4}{3} + \frac{9}{4} + \frac{16}{5} + \dots + \frac{100}{11}$$

$$\sum_{k=1}^{10} \frac{k^2}{k+1}$$

$$b) \frac{1}{3} + \frac{2}{4} + \frac{3}{5} + \frac{4}{6} + \dots + \frac{8}{10}$$

$$\sum_{k=1}^8 \frac{k}{k+2}$$

$$c) 5 + 9 + 13 + \dots + 137$$

Arithmetic Series  $\rightarrow \sum_{k=1}^n mx+b$

$$t_n = a + (n-1)d$$

$$137 = 5 + (n-1)(4)$$

$$\frac{132}{4} = n-1$$

$$33+1 = \underline{\underline{n=34}}$$

$$\sum_{k=1}^{34} (mk+b)$$

$$\sum_{k=1}^{34} (4k+1)$$

$d=4$

$$d) 23 + 19 + 15 + \dots + (-305)$$

$$\sum_{k=1}^n -4k + \square$$

$$t_n = a + (n-1)d$$

$$-305 = 23 + (n-1)(-4)$$

$$\frac{-328}{-4} = n-1$$

$$82 = n-1$$

$$n = \underline{\underline{83}}$$

$$\sum_{k=1}^{83} (-4k+27)$$

$d=-4$

$$P_{10} \rightarrow 5,6$$

$$P_{18} \rightarrow 3,5$$

## Chp 1 Review

1989-1996

2012-2013

- ① Determine the first term and common difference of the following arithmetic sequence:  $t_{50} = 140$  and  $t_{70} = 180$

$$t_n = a + (n-1)d$$

$$140 = a + 49d \quad (1)$$

$$180 = a + 69d \quad (2)$$

$$(1) - (2) \quad -40 = -20d$$

$$d = 2$$

$$140 = a + 49(2)$$

$$140 - 98 = a$$

$$a = 42$$

- ② Determine  $r$  and  $a$  for the following geometric sequence:  
 $t_3 = 99$  and  $t_5 = 11$ .

$$t_n = ar^{n-1}$$

$$99 = ar^2 \quad (1)$$

$$11 = ar^4 \quad (2) \rightarrow 11 = a\left(\pm\frac{1}{3}\right)^4$$

$$(1) \div (2) \quad 9 = r^{-2} \quad 11 = a\left(\frac{1}{81}\right)$$

$$\frac{1}{9} = r^2$$

$$r = \pm\frac{1}{3}$$

$$(11)(81) = a$$

$$891 = a$$

- ③ Determine the sum of the arithmetic series:  $20 + 14 + 8 + \dots - 70$

$$S_n = \frac{n}{2}(a + l)$$

$$t_n = a + (n-1)d$$

$$-70 = 20 + (n-1)(-6)$$

$$\frac{-90}{-6} = n-1$$

$$15 = n-1$$

$$n = 16$$

$$S_{16} = \frac{16}{2}(20 + (-70))$$

$$S_{16} = 8(-50)$$

$$S_{16} = -400$$

- ④ Determine the sum:  $17 - 51 + 153 - \dots - 334611$

$$a = 17$$

$$r = -3$$

$$l = -334611$$

$$S_n = \frac{a - rl}{1 - r}$$

$$S_n = \frac{17 - (-3)(-334611)}{1 - (-3)}$$

$$= \frac{17 - 1003833}{4} = \frac{-250954}{4}$$

$$* \text{By } 376 \text{ } \frac{-250954}{4} = -64487.25$$



5) Determine the number of terms algebraically (Day 2)

$$1, 3x^2, 9x^4, \dots, 243x^{10}$$

$$a = 1$$

$$r = 3x^2$$

$$L_n = l = 243x^{10}$$

$$L_n = ar^{n-1}$$

$$243x^{10} = 1(3x^2)^{n-1}$$

$$243x^{10} = (3x^2)^{n-1}$$

$$(3x^2)^3 = (3x^2)^{n-1}$$

$$5 = n - 1$$

$$n = 6$$

OR

$$x^{10} = x^{2(n-1)}$$

$$10 = 2n - 2$$

$$12 = 2n$$

$$n = 6$$

5) Determine whether convergent or divergent and state the sum where possible

$$a) \frac{5}{12} - \frac{5}{6} + \frac{5}{3} - \frac{10}{3} + \dots$$

$$r = \frac{-5}{6}$$

$$\frac{5}{12}$$

$$r = -2$$

NO FINITE SUM / DIVERGENT

6)  $-64 + 16 - 4 + \dots$

$$r = \frac{16}{-64}$$

$$r = -\frac{1}{4}$$

CONVERGENT

$$*P_9 40 * 1 - 53$$

$$\frac{-64}{1.25} = \underline{\underline{-51.2}}$$

7) The sum of an infinite series is 120 and the common ratio is  $-\frac{2}{5}$ . Determine the first three terms of the series.

$$S_\infty = \frac{a}{1-r}$$

$$120 = \frac{a}{1 - (-\frac{2}{5})} \quad 120 = \frac{a}{1.4}$$

$$a = (120)(1.4) = 168$$

$$120 = \frac{a}{1 + \frac{2}{5}}$$

$$\left(x \frac{2}{5}\right) \left(x \frac{2}{5}\right) \left(x \frac{2}{5}\right)$$

$$168, -67.2, 26.88$$

8) Bouncing Ball: 6.5m, 47%

a) Comes to rest

$$S = 2 \left( \frac{a}{1-r} \right) - a$$

$$S = 2 \left( \frac{6.5}{1-0.47} \right) - 6.5$$

$$S = \underline{\underline{18.03m}}$$

b) 7th bounce

$$S = 2 \left( \frac{a(1-r^n)}{1-r} \right) - a$$

$$S = 2 \left( \frac{6.5(1-0.47^7)}{1-0.47} \right) - 6.5$$

$$S = \underline{\underline{17.90m}}$$

Pg 40

# 1-53

\* When making sigma:

Arithmetic:  $\sum_{k=1}^n mk + b$

Geometric:  $\sum_{k=1}^n ar^{k-1}$

$2(x) - a$

$\sum_{k=1}^n$

$\sum_{k=1}^n$   
 $2(x)$