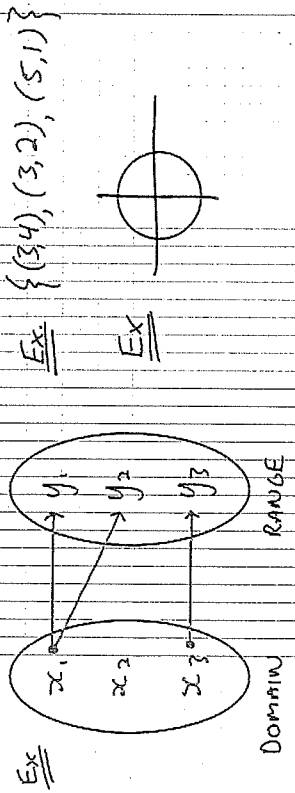
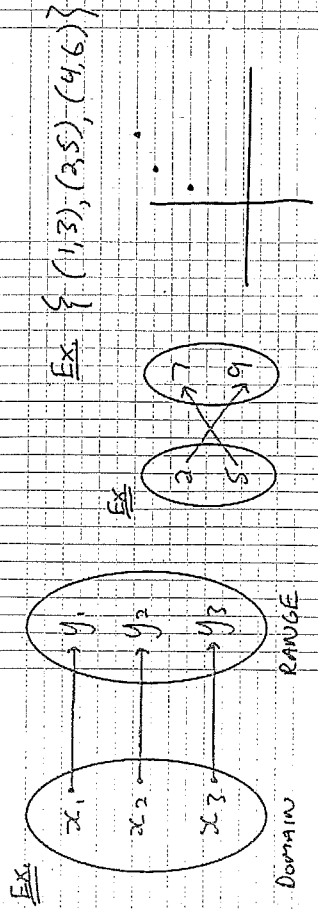


1.1 Functions and Relations

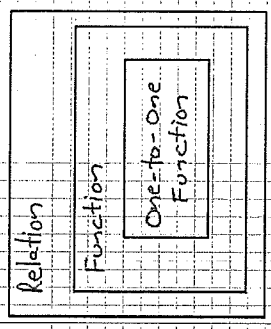
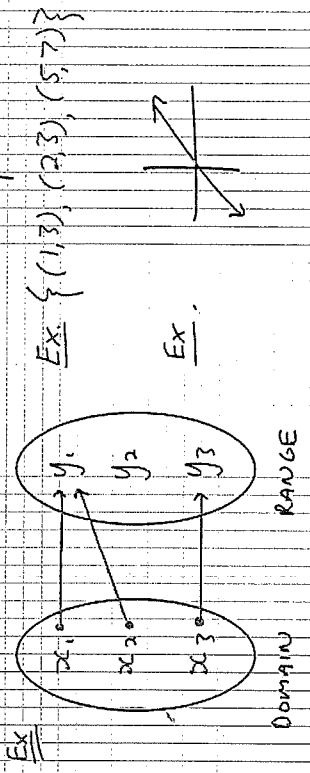
Relation - a rule/equation that produces one or more output (y-values) numbers for every valid input (x-values) numbers



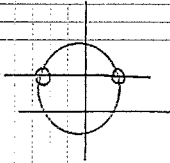
One-to-One Function - a function in which every x-value is associated with one y-value and vice versa.



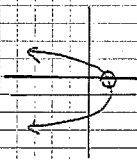
Function - for every input (x-value) number, there is only one output (y-value) number.



Vertical Line Test - used to determine whether or not a graph is a function.



NOT A FUNCTION

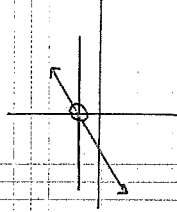


FUNCTION

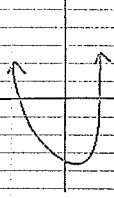
Horizontal Line Test - used to determine whether or not a function is a one-to-one function.



NOT ONE-TO-ONE



ONE-TO-ONE FUNCTION

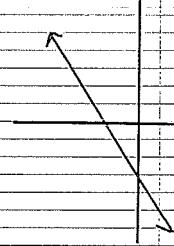


NOT A FUNCTION  
 $\therefore$  NOT ONE-TO-ONE  
 $\therefore$  RELATION

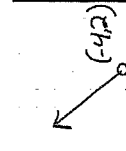
DOMAIN - the domain of a function is the set of all possible  $x$ -values (independent values)

RANGE - the range of a function is the set of all possible  $y$ -values (dependent values)

(1)



(2)



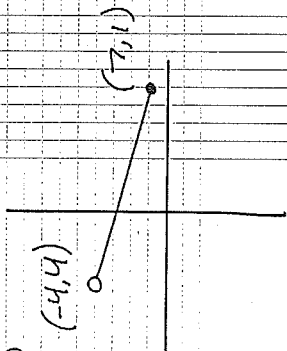
D:  $x \in \mathbb{R}$  or  $(-\infty, \infty)$

R:  $y \in \mathbb{R}$  or  $(-\infty, \infty)$

D:  $x < -4$  or  $(-\infty, -4)$

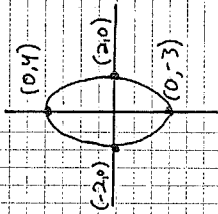
R:  $y > 2$  or  $(2, \infty)$

3



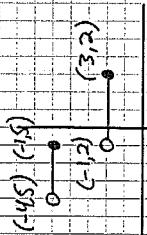
D:  $-4 < x \leq 7$  or  $(-4, 7]$   
 R:  $1 \leq y < 4$  or  $[1, 4)$

4



D:  $-2 \leq x \leq 2$  or  $[-2, 2]$   
 R:  $-3 \leq y \leq 4$  or  $[-3, 4]$

5



D:  $-4 < x \leq 3$  or  $(-4, 3]$   
 R:  $\{0, 5\}$

Ry  
 # 2, 3

ANSWER CORRECTIONS:

2) Neither  
 i) - function

3f)  $0 \leq y \leq 1$

## 1.2 Arithmetic Combinations of Functions

SUM  $(f+g)(x) = f(x) + g(x)$

DIFFERENCE  $(f-g)(x) = f(x) - g(x)$

PRODUCT  $(fg)(x) = f(x) \cdot g(x)$

QUOTIENT  $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, g(x) \neq 0$

b)  $(i-g)(x)$

$$i(x) - g(x) = 3 - (x^2 - 4x + 3)$$

$$= 3 - x^2 + 4x - 3$$

$$= \boxed{-x^2 + 4x}$$

$f(x) = 3x + 2, g(x) = x^2 - 4x + 3, h(x) = x^3, i(x) = 3$

① Given  $f(x) = 3x + 2, g(x) = x^2 - 4x + 3, h(x) = x^3, i(x) = 3$

determine:

a)  $(f+g)(x)$

$$f(x) + g(x) = 3x + 2 + x^2 - 4x + 3$$

$$= \boxed{x^2 - x + 5}$$

c)  $[h \cdot (f+g)](x)$

$$h(x) [f(x) + g(x)]$$

$$= x^3 [x^2 - x + 5]$$

$$= \boxed{x^5 - x^4 + 5x^3}$$

$f(x) = 3x + 2, g(x) = x^2 - 4x + 3, h(x) = x^3, i(x) = 3$

$$d) \left(\frac{ig}{h}\right)(2)$$

$$\frac{i(2)g(2)}{h(2)} = \frac{(3)(-1)}{8} = -\frac{3}{8}$$

$$f(x) = 3x + 2, g(x) = x^2 - 4x + 3, h(x) = x^3, i(x) = 3$$

$$e) (fi)(2) - (hg)(-1)$$

$$f(2)i(2) - h(-1)g(-1)$$

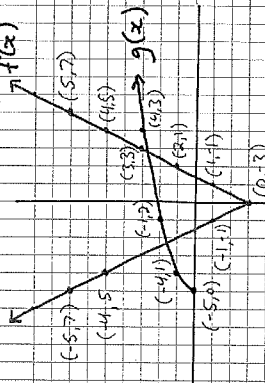
$$(8)(3) - (-1)(8)$$

$$24 - (-8)$$

$$32$$

$$f(x) = 3x + 2, g(x) = x^2 - 4x + 3, h(x) = x^3, i(x) = 3$$

2) Use the graphs of  $f(x)$  and  $g(x)$  to evaluate each function:



$$f(2) + g(4)$$

$$1 + 3$$

$$\boxed{4}$$

$$a) (f+g)(4)$$

$$b) (f+g)(-5)$$

$$c) (fg)(-4)$$

$$a) (f+g)(4)$$

$$f(4) + g(4)$$

$$5 + 3$$

$$\boxed{8}$$

$$b) (f+g)(-5)$$

$$f(-5) + g(-5)$$

$$7 + 0$$

$$\boxed{7}$$

$$c) (fg)(-4)$$

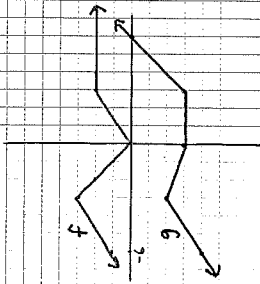
$$f(-4)g(-4)$$

$$(5)(1)$$

$$\boxed{5}$$

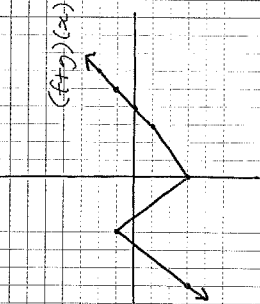
③  $f \cdot 5 * 5$  (a,e)

a)  $(a) (f+g)(x)$



$f(x) + g(x)$

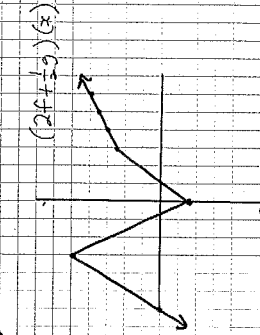
x	y
-6	-3
-3	1
0	-3
3	-1
4	0
5	1
6	2



b) (e)  $(2f + \frac{1}{2}g)(x)$

$2f(x) + \frac{1}{2}g(x) \rightarrow 2(1) + \frac{1}{2}(4)$

x	y
-6	0
-3	5
0	-1.5
3	2.5
4	3
5	3.5
6	4



$f \cdot 13$

\* 1-3 (a,e,g)

4-6 (a,e)

7,8 (d,e)

### 1.3 Composite Functions

NRU THM

6/26/2012

The composition of  $f(x)$  and  $g(x)$  is defined as  $f(g(x))$  and is formed when the equation of  $g(x)$  is substituted into the equation of  $f(x)$ .

$$f(g(x)) = (f \circ g)(x)$$

$$g(f(x)) = (g \circ f)(x)$$

1) If  $f(x) = 2 - x^2$  and  $g(x) = 3x + 2$ , find

a)  $(f \circ g)(x)$

$$\begin{aligned} f(g(x)) &= 2 - (3x+2)^2 \\ &= 2 - (3x+2)(3x+2) \\ &= 2 - (9x^2 + 12x + 4) \\ &= \boxed{-9x^2 - 12x - 2} \end{aligned}$$

b)  $(g \circ f)(x)$   $f(x) = 2 - x^2$  and  $g(x) = 3x + 2$

$$\begin{aligned} g(f(x)) &= 3(2 - x^2) + 2 \\ &= 6 - 3x^2 + 2 \\ &= \boxed{-3x^2 + 8} \end{aligned}$$

c)  $(g \circ g)(x)$

$$f(x) = 2 - x^2 \quad g(x) = 3x + 2$$

$$\begin{aligned} g(g(x)) &= 3(3x+2) + 2 \\ &= 9x + 6 + 2 \\ &= \boxed{9x + 8} \end{aligned}$$

② If  $f(x) = 3x + 4$  and  $g(x) = x^2 - 1$ , determine:

a)  $f(g(1))$       b)  $(f \circ g)(-2)$       c)  $(g \circ f)(-3)$

$= f(1^2 - 1)$        $= f(g(-2))$        $= g(f(-3))$

$= f(0)$        $= f((-2)^2 - 1)$        $= g(3(-3) + 4)$

$= 3(0) + 4$        $= f(3)$        $= g(-5)$

$= 4$        $= 3(3) + 4$        $= (-5)^2 - 1$

$= 13$        $= 24$

③ Given  $f(x) = x - 1$ ,  $g(x) = 4$ ,  $h(x) = \frac{x+1}{x-1}$  evaluate

$(h \circ g \circ f)(-2)$

$= (h(g(f(-2))))$

$= (h(g(-3)))$

$= (h(4))$

$= \frac{5}{3}$

④ If  $f(x) = \frac{x}{x-1}$  and  $g(x) = \frac{1}{x+1}$  find:

a)  $(f \circ g)(x)$  and its domain

$f(g(x)) = f\left(\frac{1}{x+1}\right) = \frac{1}{\frac{1}{x+1} - 1}$

$= \frac{1}{\frac{1}{x+1} - 1} = \frac{1}{\frac{1 - (x+1)}{x+1}} = \frac{1}{\frac{-x}{x+1}} = \frac{x+1}{-x}$

$= \frac{x+1}{-x} = \frac{1}{-x} \text{ or } -\frac{1}{x}$

D:  $x \neq 0, \neq 1$

b)  $(g \circ f)(x)$        $f(x) = \frac{x}{x-1}$  and  $g(x) = \frac{1}{x+1}$

$g(f(x)) = g\left(\frac{x}{x-1}\right)$

$= \frac{1}{\frac{x}{x-1} + 1} = \frac{1}{\frac{x + x-1}{x-1}} = \frac{1}{\frac{2x-1}{x-1}}$

D:  $x \neq \frac{1}{2}, \neq 1$



5) If  $f = \{(2,3), (3,5), (4,1), (5,0)\}$  determine:  
 $g = \{(3,7), (4,5), (5,3), (6,1)\}$

a)  $f \circ g$   
 b)  $g \circ f$

$$g(3) = 7 \rightarrow f(7) = \emptyset$$

$$g(4) = 5 \rightarrow f(5) = 0 \therefore (4,0)$$

$$g(5) = 3 \rightarrow f(3) = 5 \therefore (5,5)$$

$$g(6) = 1 \rightarrow f(1) = \emptyset$$

$$\therefore f \circ g = \{(4,0), (5,5)\}$$

$$f(2) = 3 \rightarrow g(3) = 7 \quad (2,7)$$

$$f(3) = 5 \rightarrow g(5) = 3 \quad (3,3)$$

$$\therefore g \circ f = \{(2,7), (3,3)\}$$

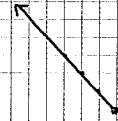
6) Find two functions  $f(x)$  and  $g(x)$  such that  
 $h(x) = (f \circ g)(x)$ .

a)  $h(x) = \frac{2}{x^2+4}$   
 b)  $h(x) = 3\sqrt{3x^2-2}$

$f(x) = \frac{2}{x}$   
 $g(x) = x^2+4$   
 $f(x) = 3\sqrt{x}$   
 $g(x) = 3x^2-2$   
 $f(x) = 3\sqrt{3x^2}$   
 $g(x) = 3x^2$

6) Given  $f(x) = x^2+2$  and  $g(x) = \sqrt{x-2}$  sketch  
 $(f \circ g)(x)$  and state the domain (Pg 246 b)

$$\begin{aligned} f(g(x)) &= f(\sqrt{x-2}) \\ &= (\sqrt{x-2})^2+2 \\ &= x-2+2 \\ &= x \\ \therefore x &\geq 2 \end{aligned}$$



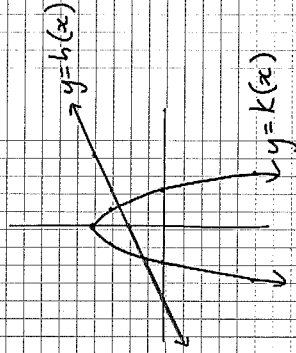
6) Determine

a)  $k(h(2))$   
 Pg 25 \* 7 d)

$$k(3) = -5$$

b)  $h(k(-1))$   
 Pg 25 \* 7 b)

$$h(3) = 3.5$$



Py 22

#2-5 (m, s, e)

6, 7 (m, s, e...)

8-10 (m, s, e)

# 1.4 TRANSFORMATIONS OF GRAPHS Pt. 1

## TRANSLATIONS

Given  $y = f(x)$

$y - k = f(x)$  OR  $y = f(x) + k$  describes a VERTICAL TRANSLATION

Ex  $y = x^2 + 4$

$y = f(x - h)$  describes a HORIZONTAL TRANSLATION

Ex  $y = (x - 2)^2$

$y = f(x - h) + k$

If  $k > 0$

Moves graph up

Ex.  $y = |x| + 2 \rightarrow \text{Up } 2$

If  $k < 0$

Moves graph down

Ex.  $y = \sqrt{x} - 3 \rightarrow \text{Down } 3$

If  $h > 0$

Moves graph right

Ex.  $y = (x - 2)^2 \rightarrow \text{Right } 2$

If  $h < 0$

Moves graph left

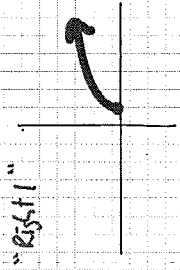
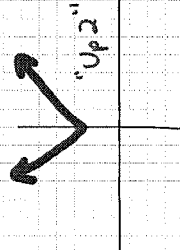
Ex.  $y = \sqrt{x+4} \rightarrow \text{Left } 4$   
 $y = \sqrt{x - (-4)}$

1) Sketch the following functions

a)  $y = (x+3)^2$

b)  $y = |x| + 2$

c)  $y = \sqrt{x-1}$



2) If  $(-5, 3)$  or  $(a, b)$  are on the graph of  $y = f(x)$ , what must be on the graph of:

a)  $y = f(x+3)$

$(x, y) \rightarrow (x-3, y)$

$(-8, 3), (a-3, b)$

b)  $y = f(x-2) - 5$

$(x, y) \rightarrow (x+2, y-5)$

$(-3, -2), (a+2, b-5)$

3) If  $(2, -4)$  or  $(a, b)$  are on the graph of  $y = f(x-2)$  what must be on the graph of:

a)  $y = f(x)$

b)  $y = f(x+1) - 2$

$(0, -4), (a-2, b)$

$(-1, -6), (a-3, b-2)$

4) If  $(-3, 2)$  or  $(a, b)$  are on the graph of  $y = f(x+1) - 4$  what must be on the graph of  $y = f(x+2) + 6$

$y = f(x) ?$

"Move Right 1 and Up 4 to get to start"

$(-2, 6) / (a+1, b+4)$

$\hookrightarrow (x-2, y+6) \rightarrow (-4, 12)$

$(a-1, b+10)$

5) Given  $y = f(x)$  sketch  $y = f(x+2) - 3$

"Mapping Points"

$(x, y) \rightarrow (x-2, y-3)$

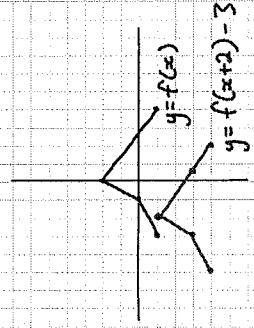
$(-3, -1) \rightarrow (-5, -4)$

$(-1, 0) \rightarrow (-3, -3)$

$(0, 2) \rightarrow (-2, -1)$

$(2.5, 0) \rightarrow (0.5, -3)$

$(4, -1) \rightarrow (2, -4)$



$(-3, -1) \rightarrow (-5, -4)$

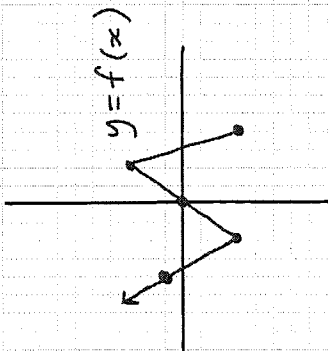
$(-1, 0) \rightarrow (-3, -3)$

$(0, 2) \rightarrow (-2, -1)$

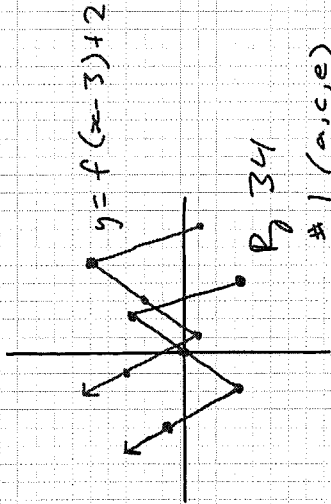
$(2.5, 0) \rightarrow (0.5, -3)$

$(4, -1) \rightarrow (2, -4)$

6) Given  $y = f(x)$ , sketch  $y = f(x-3) + 2$



- $(x, y) \rightarrow (x+3, y+2)$
- $(-4, 1) \rightarrow (-1, 3)$
- $(-2, -3) \rightarrow (1, -1)$
- $(0, 0) \rightarrow (3, 2)$
- $(2, 3) \rightarrow (5, 5)$
- $(4, -3) \rightarrow (7, -1)$



- $(x, y) \rightarrow (x+3, y+2)$
- $(-4, 1) \rightarrow (-1, 3)$
- $(-2, -3) \rightarrow (1, -1)$
- $(0, 0) \rightarrow (3, 2)$
- $(2, 3) \rightarrow (5, 5)$
- $(4, -3) \rightarrow (7, -1)$

P 34

# 1 (a, c, e)

2 (a, b, c)

9 (d, e)

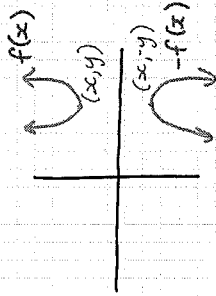
10 (a, d, e)

# 1.4 Transformations Pt. 2

INFORM ENG 201-01-28

## REFLECTIONS

### Reflection in/cross the x-axis



$$f(x) \rightarrow -f(x)$$

Ex  $f(x) = x^3 - x^2 + 2$   
 $-f(x) = -(x^3 - x^2 + 2)$   
 $= -x^3 + x^2 - 2$

MAPPING OF POINTS

$$(x, y) \rightarrow (x, -y)$$

### Reflection in/cross the y-axis

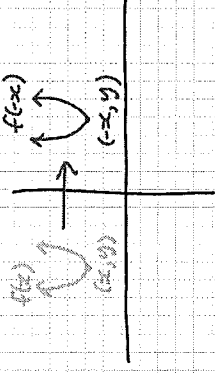
$$f(x) \rightarrow f(-x)$$

Ex  $f(x) = x^3 - x^2 + 2$

$$(x, y) \rightarrow (-x, y)$$

$$f(-x) = (-x)^3 - (-x)^2 + 2$$

$$f(-x) = -x^3 - x^2 + 2$$



## COMPRESSIONS AND EXPANSIONS

Given  $y = a f(bx)$

$a$  affects the y-coordinate (Vertical)

$b$  affects the x-coordinate (Horizontal)

$$y = a f(b(x-h)) + k$$

$a > 1$  Vertical Expansion

$0 < a < 1$  Vertical Compression

$a < 0$  Reflection in x-axis

$b > 1$  Horizontal Compression

$0 < b < 1$  Horizontal Expansion

$b < 0$  Reflection in y-axis

$$y = 2f(x) \text{ vert exp. } \times 2$$

$(x, y) \rightarrow (x, 2y)$

$$y = \frac{1}{3}f(x) \text{ vert. compr. } \times \frac{1}{3}$$

$(x, y) \rightarrow (x, \frac{1}{3}y)$

$$y = -f(x)$$

$(x, y) \rightarrow (x, -y)$

$$y = f(3x) \text{ horiz. compr. } \times \frac{1}{3}$$

$(x, y) \rightarrow (\frac{1}{3}x, y)$

$$y = f(\frac{1}{4}x) \text{ horiz. exp. } \times 4$$

$(x, y) \rightarrow (4x, y)$

$$y = f(-x)$$

$(x, y) \rightarrow (-x, y)$

1) Map the point and write the equation of the image of  $y = f(x)$  after each transformation.

a) A horizontal expansion by a factor of 5 and a reflection in the  $y$ -axis.

$$(x, y) \rightarrow (-5x, y) \quad y = f\left(-\frac{1}{5}x\right)$$

b) A vertical compression by a factor of  $\frac{2}{3}$  and a horizontal compression by a factor of  $\frac{4}{7}$

$$(x, y) \rightarrow \left(\frac{4}{7}x, \frac{2}{3}y\right) \quad y = \frac{2}{3}f\left(\frac{7}{4}x\right)$$

2) Write the equation for each function:  $y = a f(b(x-h)) + k$

a)  $f(x) = x^2$ , moved 4 units to the left, vertically expanded  $\times 2$ , and 3 units down.

$$y = 2f(x+4) - 3$$

↓

$$y = 2(x+4)^2 - 3 \quad (x, y) \rightarrow (x-4, 2y-3)$$

b)  $f(x) = |x|$ , moved 5 units to the right, horizontally compressed  $\times \frac{1}{3}$ , and reflected across the  $x$ -axis.

$$y = -f(3(x-5))$$

↓

$$y = -|3(x-5)| \rightarrow y = -|3x-15|$$

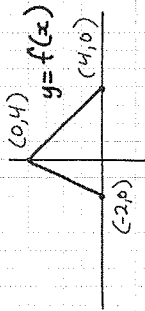
$$(x, y) \rightarrow \left(\frac{1}{3}x+5, -y\right)$$

c)  $f(x) = \sqrt{x}$ , moved 2 units left and 3 units up, horizontally expanded by 6, vertically compressed by  $\frac{1}{4}$ , and reflected in the  $y$ -axis.

$$y = \frac{1}{4}\sqrt{-\frac{1}{6}(x+2)} + 3$$

$$(x, y) \rightarrow (-6x-2, \frac{1}{4}y+3)$$

3) Given  $y = f(x)$ , sketch the following:



a)  $y = -f(\frac{1}{2}x)$     b)  $y = 2f(-2x)$     c)  $y = -\frac{1}{2}f(x+1) + 3$   
 $(x, y) \rightarrow (2x, -y)$      $(x, y) \rightarrow (\frac{1}{2}x, 2y)$      $(x, y) \rightarrow (x-1, \frac{1}{2}y+3)$

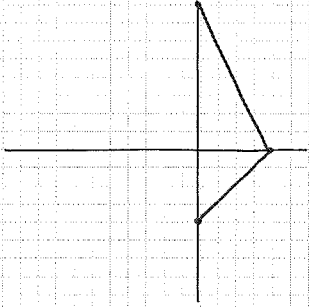
a)  $y = -f(\frac{1}{2}x) \rightarrow$  Reflected in x-axis, Horiz. Exp  $\times 2$

$(x, y) \rightarrow (2x, -y)$

$(-2, 0) \rightarrow (-4, 0)$

$(0, 4) \rightarrow (0, -4)$

$(4, 0) \rightarrow (8, 0)$



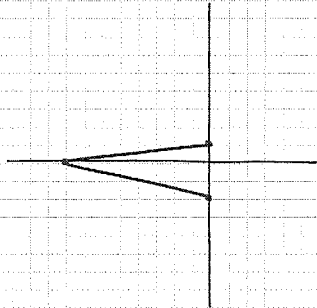
b)  $y = 2f(-2x) \rightarrow$  Vert. Expanded  $\times 2$ , Horiz. Comp.  $\times \frac{1}{2}$ ,  
 Reflected in y-axis

$(x, y) \rightarrow (-\frac{1}{2}x, 2y)$

$(-2, 0) \rightarrow (1, 0)$

$(0, 4) \rightarrow (0, 8)$

$(4, 0) \rightarrow (-2, 0)$

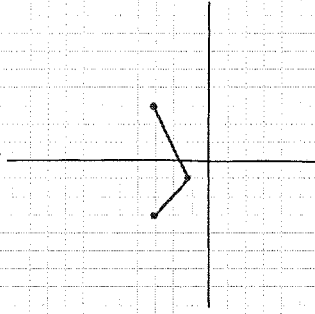


c)  $y = -\frac{1}{2}f(x+1) + 3$   
 $(x, y) \rightarrow (x-1, -\frac{1}{2}y+3)$

$(-2, 0) \rightarrow (-3, 3)$

$(0, 4) \rightarrow (-1, 1)$

$(4, 0) \rightarrow (3, 3)$



Ry 34

# 1, 2 (d, f, h)

11, 12



## 1.5 Inverse Functions

Math Title

8/27/2012

To determine the inverse  $f^{-1}(x)$  of a function  $f(x)$ :

1. Interchange  $x$  and  $y$
2. Solve for  $y$ 
  - Mapping of points for  $f^{-1}(x)$ :  $(x, y) \rightarrow (y, x)$
  - The graphs of  $f(x)$  and  $f^{-1}(x)$  are symmetric about the line  $y = x$

$$b) f(x) = \frac{2x-1}{3x+2}$$

$$x = \frac{2y-1}{3y+2}$$

$$x(3y+2) = 2y-1$$

$$3xy + 2x - 2y = -1$$

$$3xy - 2y = -1 - 2x$$

$$y(3x-2) = -1-2x$$

$$y = \frac{-1-2x}{3x-2} \quad \text{or} \quad f^{-1}(x) = \frac{-1-2x}{3x-2}$$

① Determine  $f^{-1}(x)$

$$a) f(x) = 3x-2$$

$$y = 3x-2$$

$$x = 3y-2$$

$$x+2 = 3y$$

$$\frac{x+2}{3} = y$$

$$y = \frac{x+2}{3}$$

$$f^{-1}(x) = \frac{x+2}{3}$$

Two functions  $f(x)$  and  $g(x)$  are inverses of each other if:

$$f[g(x)] = x \quad \text{and} \quad g[f(x)] = x$$

\* Note: If  $f(x)$  is not one-to-one, its inverse will not be a function

Ex Given  $y = x^2 + 2$  its inverse will not be a function

$$y \rightarrow -x$$

② Determine whether the following are inverses of each other.

a)  $f(x) = x^3 - 2$ ,  $g(x) = \sqrt[3]{x+2}$

$$\begin{aligned} f[g(x)] &= \\ &= \sqrt[3]{(\sqrt[3]{x+2})^3 - 2} \\ &= \sqrt[3]{x+2-2} \\ &= \sqrt[3]{x^3} \\ &= x \checkmark \end{aligned}$$

Yes they are inverses of each other

b)  $f(x) = \sqrt[4]{x}$ ,  $g(x) = x^4$

$$f[g(x)] = f(x^4) = \sqrt[4]{x^4} = x \checkmark$$

$$\begin{aligned} g[f(x)] &= g(\sqrt[4]{x}) \\ &= (\sqrt[4]{x})^4 \\ &= x \checkmark \end{aligned}$$

No, not inverses of each other

③ If  $(-2, 3)$  is on the graph of  $y = f(x)$ , what must be a point on the graph for:

a)  $y = f^{-1}(x) + 4$  \* Swap points first

$$(x, y) \rightarrow (y, x) \rightarrow (y, x+4)$$

$$(-2, 3) \rightarrow (3, -2) \rightarrow (3, 2)$$

$$(3, 2)$$

b)  $y = -f^{-1}(x-5)$   $(-2, 3) \rightarrow ?$

$$(x, y) \rightarrow (y, x) \rightarrow (y+5, -x)$$

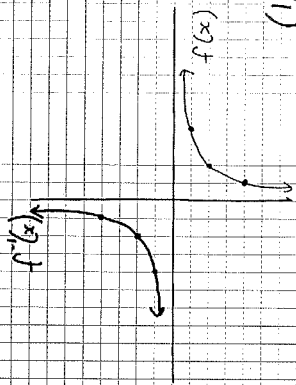
$$(-2, 3) \rightarrow (3, -2) \rightarrow (3, 2) \rightarrow (8, 2)$$

$$c) y = f^{-1}(x+2) - 3 \quad (-2, 3) \rightarrow ?$$

$$(x, y) \rightarrow (y, x) \rightarrow (y-2, x-3)$$

$$(-2, 3) \rightarrow (3, -2) \rightarrow \boxed{(1, -5)}$$

4) Given the graph of  $f(x)$  graph its inverse  $f^{-1}(x)$



By 44

$$\neq 1(21)$$

$$2, 3, 6, 7 (a, c, e)$$

$$9, 10, 11$$

$$\neq 7(2) (0, -1)$$

$$(1, -4) \rightarrow (-4, 1)$$

$$(2, -2) \rightarrow (-2, 2)$$

$$(4, -1) \rightarrow (-1, 4)$$

## 1.6 Combined Transformations

The order in which transformations are performed is important

when:

\* a translation and a stretch in the same direction are combined.

i.e. horizontal translation and horizontal compression

Follow this order: ① FACTOR  $f(2x+5)$   
 $f(2(x+\frac{5}{2}))$

② C - Compression/Expansion

③ R - Reflections

④ T - Translations

Ex: Given:  $y = f(3x-3) \Rightarrow y = f(3(x-1))$

C - Horiz. Comp.  $\times \frac{1}{3}$

R -

T - Right 1

$$(x, y) \rightarrow (\frac{1}{3}x, y) \rightarrow (\frac{1}{3}x+1, y)$$

① Show a mapping of the points for:

$$a) y = f(-2x+8) - 14$$

$$y = f(-2(x-4)) - 14$$

C - Horiz. Comp.  $\times \frac{1}{2}$

R - y-axis

T - Right 4, Down 14

$$(x, y) \rightarrow (\frac{1}{2}x, y)$$

↓

$$(-\frac{1}{2}x, y)$$

↓

$$(-\frac{1}{2}x+4, y-14)$$

$$b) y = -\frac{1}{6}f(\frac{1}{2}x+2) + 5$$

$$y = -\frac{1}{6}f(\frac{1}{2}(x+4)) + 5$$

C - Vert. Comp.  $\times \frac{1}{6}$ , Horiz. Exp.  $\times 2$

R - x-axis

T - Left 4, Up 5

$$(x, y) \rightarrow (2x, \frac{1}{6}y) \rightarrow (2x, \frac{1}{6}y)$$

↓

$$(2x-4, \frac{1}{6}y+5)$$

2. If the point  $(6, -12)$  is on the graph of  $y = f(x)$ , which point must be on the graph of  $y = f\left(-\frac{1}{3}x + 6\right)$ ?

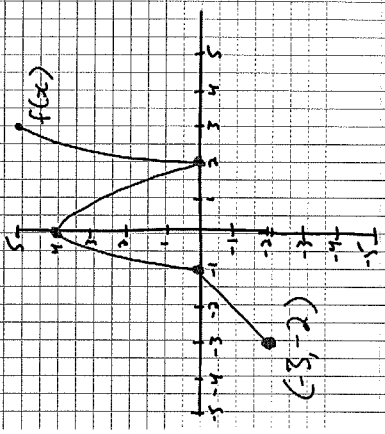
- A.  $(-36, -12)$
- B.  $(-24, -12)$
- C.  $(0, -12)$
- D.  $(16, -12)$

$$y = f\left(-\frac{1}{3}(x-18)\right)$$

$$(x, y) \rightarrow (-3x+18, y)$$

$(0, -12)$   
 C

3. Given  $y = f(x)$ , sketch  $y+4 = -\frac{1}{2}f(x+2)$



$$y = -\frac{1}{2}f(x+2) - 4$$

C - vert. comp.  $\times \frac{1}{2}$   
 R - reflection in  $x$ -axis  
 T - left 2, down 4

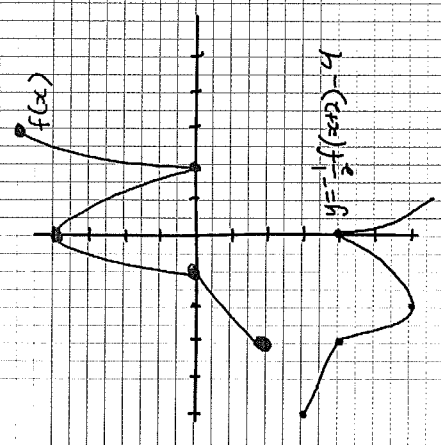
$$(x, y) \rightarrow (x, \frac{1}{2}y) \rightarrow (x, -\frac{1}{2}y) \rightarrow (x-2, -\frac{1}{2}y-4)$$

$$y = -\frac{1}{2}f(x+2) - 4$$

C - vert. comp.  $\times \frac{1}{2}$   
 R - reflection in  $x$ -axis  
 T - left 2, down 4

$$(x, y) \rightarrow (x, \frac{1}{2}y) \rightarrow (x, -\frac{1}{2}y) \Rightarrow (x-2, -\frac{1}{2}y-4)$$

- $(-3, -2) \rightarrow (-5, -3)$
- $(-1, 0) \rightarrow (-3, -4)$
- $(0, 1) \rightarrow (-2, -6)$
- $(2, 0) \rightarrow (0, -4)$
- $(3, 5) \rightarrow (1, -6.5)$



Ry 51

# 1-3 (a, c, e...)

7

REVIEW

Ry 54

# 1-65

\* Not # 4, 21, 37, 63