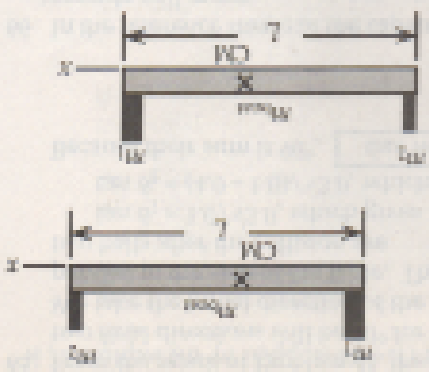


70. We choose the origin of our coordinate system at the initial position of the 75-kg person. For the location of the center of mass of the system we have

$$x_{CM} = \frac{(m_1x_1 + m_2x_2 + m_3x_3)}{(m_1 + m_2 + m_3)}$$

$$= \frac{[(75 \text{ kg})(0) + (60 \text{ kg})(2.0 \text{ m}) + (60 \text{ kg})(1.0 \text{ m})]}{(75 \text{ kg} + 60 \text{ kg} + 60 \text{ kg})} = 0.93 \text{ m}$$

Thus the CM will be  $2.0 \text{ m} - 0.93 \text{ m} = 1.07 \text{ m}$  from the 60-kg person. When the two people exchange seats, the CM will not move. The end where the 75-kg person started, which was  $0.93 \text{ m}$  from the CM, is now  $1.07 \text{ m}$  from the CM, that is, the boat must have moved  $1.07 \text{ m} - 0.93 \text{ m} = 0.14 \text{ m}$  toward the initial position of the 75-kg person.



71. (a) We take the direction of the meteor for the positive direction. For this perfectly inelastic collision, we use momentum conservation:

$$M_{\text{meteor}}v_{\text{meteor}} + M_{\text{Earth}}v_{\text{Earth}} = (M_{\text{meteor}} + M_{\text{Earth}})v_f$$

$$(10^6 \text{ kg})(15 \times 10^3 \text{ m/s}) + 0 = (10^6 \text{ kg} + 6.0 \times 10^{24} \text{ kg})v_f, \text{ which gives } v_f = 2.5 \times 10^{-13} \text{ m/s}$$

(b) The fraction transformed was

$$\frac{v_f^2}{v_{\text{meteor}}^2} = \frac{\Delta K_{\text{Earth}}/\Delta K_{\text{meteor}}}{v_{\text{meteor}}^2} = \frac{(6.0 \times 10^6 \text{ kg})(2.5 \times 10^{-13} \text{ m/s})^2 / (10^6 \text{ kg})(15 \times 10^3 \text{ m/s})^2}{1} = 1.7 \times 10^{-10}$$

(c) The change in the Earth's kinetic energy was

$$\Delta K_{\text{Earth}} = \frac{1}{2}m_{\text{Earth}}v_f^2 = \frac{1}{2}(6.0 \times 10^{24} \text{ kg})(2.5 \times 10^{-13} \text{ m/s})^2 = 0.19 \text{ J}$$

72. Momentum conservation gives

$$0 = m_1v_1' + m_2v_2', \text{ or } v_2'/v_1' = -m_1/m_2$$

The ratio of kinetic energies is

$$\frac{K_2'/K_1'}{v_2'/v_1'} = \frac{\frac{1}{2}m_2v_2'^2 / \frac{1}{2}m_1v_1'^2}{-m_1/m_2} = 2$$

When we use the result from momentum, we get

$$(m_2/m_1)(K_2'/K_1') = 2, \text{ which gives } m_1/m_2 = 2$$

73. (b) The force would become zero at

$$F = 580/(1.8 \times 10^2) = 3.22 \times 10^{-2} \text{ N}$$

At  $t = 3.0 \times 10^{-2} \text{ s}$ , the force is

$$580 - (1.8 \times 10^2)(3.0 \times 10^{-2}) = 40 \text{ N}$$

The impulse is the area under the  $F$  vs.  $t$  curve, and consists of a triangle and a rectangle:

$$\text{Impulse} = \frac{1}{2}(580 \text{ N} - 40 \text{ N})(3.0 \times 10^{-2} \text{ s}) + (40 \text{ N})(3.0 \times 10^{-2} \text{ s}) = 0.93 \text{ N} \cdot \text{s}$$

(c) We find the mass of the bullet from

$$\text{Impulse} = \Delta p = m \Delta v$$

$$0.93 \text{ N} \cdot \text{s} = m(220 \text{ m/s} - 0), \text{ which gives } m = 4.23 \times 10^{-2} \text{ kg} = 42 \text{ g}$$
