

74. We find the speed for falling or rising through a height h from energy conservation:

$$\frac{1}{2}mv^2 = mgh, \text{ or } v^2 = 2gh.$$

- (a) The speed of the first block after sliding down the incline and just before the collision is

$$v_1 = [2(9.80 \text{ m/s}^2)(3.60 \text{ m})]^{1/2} = 8.40 \text{ m/s}.$$

For the elastic collision of the two blocks, we use momentum conservation:

$$mv_1 + Mv_2 = mv_1' + Mv_2',$$

$$(2.20 \text{ kg})(8.40 \text{ m/s}) + (7.00 \text{ kg})(0) = (2.20 \text{ kg})v_1' + (7.00 \text{ kg})v_2'.$$

Because the collision is elastic, the relative speed does not change:

$$v_1 - v_2 = -(v_1' - v_2'), \text{ or } 8.40 \text{ m/s} - 0 = v_2' - v_1'.$$

Combining these two equations, we get

$$v_1' = -4.38 \text{ m/s}, \quad v_2' = 4.02 \text{ m/s}.$$

- (b) We find the height of the rebound from

$$v_1'^2 = 2gh',$$

$$(-4.38 \text{ m/s})^2 = 2(9.80 \text{ m/s}^2)h', \text{ which gives } h' = 0.979 \text{ m}.$$

The distance along the incline is

$$d = h'/\sin \theta = (0.979 \text{ m})/\sin 30^\circ = \boxed{1.96 \text{ m}}.$$



75. Because energy is conserved for the motion up and down the incline, mass m will return to the level with the speed $-v_1'$. For a second collision to occur, mass m must be moving faster than mass M : $-v_1' \geq v_2'$.

In the first collision, the relative speed does not change:

$$v_1 - 0 = -(v_1' - v_2'), \text{ or } -v_1' = v_2' - v_2',$$

so the condition becomes $v_1 - v_1' \geq v_2'$, or $v_1 \geq 2v_2'$.

For the first collision, we use momentum conservation:

$$mv_1 + 0 = mv_1' + Mv_2', \text{ or } v_1 - v_1' = (M/m)v_2'.$$

When we use the two versions of the condition, we get $v_1 - v_1' \geq 3v_2'$, so we need

$$(M/m) \geq 3, \text{ or } \boxed{m \leq M/3}.$$