

19. (a) The impulse is the area under the
- F
- vs.
- t
- curve.

The value of each block on the graph is

$$1 \text{ block} = (50 \text{ N})(0.01 \text{ s}) = 0.50 \text{ N} \cdot \text{s}.$$

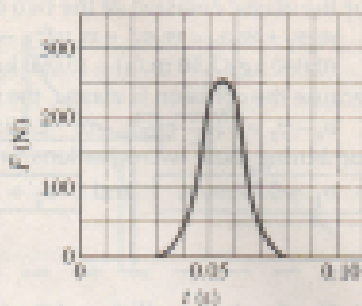
We estimate there are 10 blocks under the curve, so the impulse is

$$\text{Impulse} = (10 \text{ blocks})(0.50 \text{ N} \cdot \text{s}/\text{block}) = \boxed{5.0 \text{ N} \cdot \text{s}}.$$

- (b) We find the final velocity of the ball from

$$\text{Impulse} = \Delta p = m \Delta v:$$

$$5.0 \text{ N} \cdot \text{s} = (0.060 \text{ kg})(v - 0), \text{ which gives } v = \boxed{83 \text{ m/s}}.$$



20. The maximum force that each leg can exert without breaking is

$$(170 \times 10^6 \text{ N/m}^2)(2.5 \times 10^{-4} \text{ m}^2) = 4.25 \times 10^4 \text{ N},$$

so, if there is an even landing with both feet, the maximum force allowed on the body is $8.50 \times 10^4 \text{ N}$.

We use the work-energy principle for the fall to find the landing speed:

$$0 = \Delta K + \Delta U:$$

$$0 = \frac{1}{2}mv_{\text{land}}^2 - 0 + (0 - mgh_{\text{max}}), \text{ or } v_{\text{land}}^2 = 2gh_{\text{max}}.$$

The impulse from the maximum force changes the momentum on landing. If we take down as the positive direction and assume the landing lasts for a time t , we have

$$-F_{\text{max}}t = m \Delta v = m(0 - v_{\text{land}}), \text{ or } t = mv_{\text{land}}/F_{\text{max}}.$$

We have assumed a constant force, so the acceleration will be constant. For the landing we have

$$y = v_{\text{land}}t + \frac{1}{2}at^2 = v_{\text{land}}(mv_{\text{land}}/F_{\text{max}}) + \frac{1}{2}(-F_{\text{max}}/m)(mv_{\text{land}}/F_{\text{max}})^2 = \frac{1}{2}mv_{\text{land}}^2/F_{\text{max}} = mgh_{\text{max}}/F_{\text{max}}:$$

$$0.60 \text{ m} = (75 \text{ kg})(9.80 \text{ m/s}^2)h_{\text{max}}/(8.50 \times 10^4 \text{ N}), \text{ which gives } h_{\text{max}} = \boxed{0.69 \text{ m}}.$$

21. For the elastic collision of the two balls, we use momentum conservation:

$$m_1v_1 + m_2v_2 = m_1v_1' + m_2v_2'$$

$$(0.440 \text{ kg})(3.70 \text{ m/s}) + (0.220 \text{ kg})(0) = (0.440 \text{ kg})v_1' + (0.220 \text{ kg})v_2'$$

Because the collision is elastic, the relative speed does not change:

$$v_1 - v_2 = -(v_1' - v_2'), \text{ or } 3.70 \text{ m/s} - 0 = v_2' - v_1'.$$

Combining these two equations, we get

$$v_1' = \boxed{1.23 \text{ m/s}}, \text{ and } v_2' = \boxed{4.93 \text{ m/s}}.$$

22. For the elastic collision of the two pucks, we use momentum conservation:

$$m_1v_1 + m_2v_2 = m_1v_1' + m_2v_2'$$

$$(0.450 \text{ kg})(3.00 \text{ m/s}) + (0.900 \text{ kg})(0) = (0.450 \text{ kg})v_1' + (0.900 \text{ kg})v_2'$$

Because the collision is elastic, the relative speed does not change:

$$v_1 - v_2 = -(v_1' - v_2'), \text{ or } 3.00 \text{ m/s} - 0 = v_2' - v_1'.$$

Combining these two equations, we get

$$v_1' = \boxed{-1.00 \text{ m/s (rebound)}}, \text{ and } v_2' = \boxed{2.00 \text{ m/s}}.$$

23. For the elastic collision of the two billiard balls, we use momentum conservation:

$$m_1v_1 + m_2v_2 = m_1v_1' + m_2v_2'$$

$$m(2.00 \text{ m/s}) + m(-3.00 \text{ m/s}) = mv_1' + mv_2'$$

Because the collision is elastic, the relative speed does not change:

$$v_1 - v_2 = -(v_1' - v_2'), \text{ or } 2.00 \text{ m/s} - (-3.00 \text{ m/s}) = v_2' - v_1'.$$

Combining these two equations, we get

$$v_1' = \boxed{-3.00 \text{ m/s (rebound)}}, \text{ and } v_2' = \boxed{2.00 \text{ m/s}}.$$

Note that the two billiard balls exchange velocities.