

34. (a) For a perfectly elastic collision, we use momentum conservation:

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2', \text{ or } m_1(v_1 - v_1') = m_2(v_2' - v_2).$$

Kinetic energy is conserved, so we have

$$\frac{1}{2}m_1 v_1^2 + \frac{1}{2}m_2 v_2^2 = \frac{1}{2}m_1 v_1'^2 + \frac{1}{2}m_2 v_2'^2, \text{ or } m_1(v_1^2 - v_1'^2) = m_2(v_2'^2 - v_2^2),$$

which can be written as

$$m_1(v_1 - v_1')(v_1 + v_1') = m_2(v_2' - v_2)(v_2' + v_2).$$

When we divide this by the momentum result, we get

$$v_1 + v_1' = v_2' + v_2, \text{ or } v_1' - v_2' = v_2 - v_1.$$

If we use this in the definition of the coefficient of restitution, we get

$$e = (v_1' - v_2') / (v_2 - v_1) = (v_2 - v_1) / (v_2 - v_1) = 1.$$

For a completely inelastic collision, the two objects move together, so we have

$$v_1' = v_2', \text{ which gives } e = 0.$$

- (b) We find the speed after falling a height h from energy conservation:

$$\frac{1}{2}m v_1^2 = mgh, \text{ or } v_1 = (2gh)^{1/2}.$$

The same expression holds for the height reached by an object moving upward:

$$v_1' = (2gh')^{1/2}.$$

Because the steel plate does not move, when we take into account the directions we have

$$e = (v_1' - v_2') / (v_2 - v_1) = [(2gh')^{1/2} - 0] / [0 - (-(2gh)^{1/2})], \text{ so } \boxed{e = (h'/h)^{1/2}}.$$

35. Momentum conservation for the explosion gives us

$$0 = m_1 v_1' + m_2 v_2'$$

$$0 = m_1 v_1' + 3m_1 v_2', \text{ or } v_1' = -3v_2'.$$

On the horizontal surface after the collision, the normal force on a block is $F_N = mg$.

We relate the speed of a block immediately after the collision to the distance it slides from the

work-energy principle for the sliding motion:

$$W_N = \Delta KE;$$

$$-\mu_k mgd = 0 - \frac{1}{2}mv^2, \text{ or } d = \frac{1}{2}v^2 / \mu_k g.$$

If we use this for each block and form the ratio, we get

$$d_1/d_2 = (v_1/v_2)^2 = (-3)^2 = \boxed{9}, \text{ with the lighter block traveling farther.}$$

36. For the momentum conservation of this one-dimensional collision, we have

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'.$$

- (a) If the bodies stick together, $v_1' = v_2' = V$:

$$(5.0 \text{ kg})(5.5 \text{ m/s}) + (3.0 \text{ kg})(-4.0 \text{ m/s}) = (5.0 \text{ kg} + 3.0 \text{ kg})V, \text{ which gives } V = \boxed{v_1' = v_2' = 1.9 \text{ m/s}}.$$

- (b) If the collision is elastic, the relative speed does not change:

$$v_1 - v_2 = -(v_1' - v_2'), \text{ or } 5.5 \text{ m/s} - (-4.0 \text{ m/s}) = 9.5 \text{ m/s} = v_2' - v_1'.$$

The momentum equation is

$$(5.0 \text{ kg})(5.5 \text{ m/s}) + (3.0 \text{ kg})(-4.0 \text{ m/s}) = (5.0 \text{ kg})v_1' + (3.0 \text{ kg})v_2', \text{ or}$$

$$(5.0 \text{ kg})v_1' + (3.0 \text{ kg})v_2' = 15.5 \text{ kg} \cdot \text{m/s}.$$

When we combine these two equations, we get $\boxed{v_1' = -1.6 \text{ m/s}, v_2' = 7.9 \text{ m/s}}.$

- (c) If m_1 comes to rest, $v_1' = 0$:

$$(5.0 \text{ kg})(5.5 \text{ m/s}) + (3.0 \text{ kg})(-4.0 \text{ m/s}) = 0 + (3.0 \text{ kg})v_2', \text{ which gives } \boxed{v_1' = 0, v_2' = 3.2 \text{ m/s}}.$$

- (d) If m_2 comes to rest, $v_2' = 0$:

$$(5.0 \text{ kg})(5.5 \text{ m/s}) + (3.0 \text{ kg})(-4.0 \text{ m/s}) = (5.0 \text{ kg})v_1' + 0, \text{ which gives } \boxed{v_1' = 3.1 \text{ m/s}, v_2' = 0}.$$

- (e) The momentum equation is

$$(5.0 \text{ kg})(5.5 \text{ m/s}) + (3.0 \text{ kg})(-4.0 \text{ m/s}) = (5.0 \text{ kg})(-4.0 \text{ m/s}) + (3.0 \text{ kg})v_2',$$

which gives $\boxed{v_1' = -4.0 \text{ m/s}, v_2' = 12 \text{ m/s}}.$

The result for (c) is reasonable. The 3.0-kg body rebounds.

The result for (d) is not reasonable. The 5.0-kg body would have to pass through the 3.0-kg body.

To check the result for (e) we find the change in kinetic energy:

$$\begin{aligned} \Delta KE &= \left(\frac{1}{2}m_1 v_1'^2 + \frac{1}{2}m_2 v_2'^2 \right) - \left(\frac{1}{2}m_1 v_1^2 + \frac{1}{2}m_2 v_2^2 \right) \\ &= \frac{1}{2}[(5.0 \text{ kg})(-4.0 \text{ m/s})^2 + (3.0 \text{ kg})(12 \text{ m/s})^2] \\ &\quad - \frac{1}{2}[(5.0 \text{ kg})(5.5 \text{ m/s})^2 + (3.0 \text{ kg})(-4.0 \text{ m/s})^2] \\ &= +156 \text{ J}. \end{aligned}$$

Because the kinetic energy cannot increase in a simple collision, $\boxed{\text{the result for (e) is not reasonable.}}$