

52. The angular frequency of the SHM is

$$\omega = (k/m)^{1/2} = [(126 \text{ N/m}) / (0.800 \text{ kg})]^{1/2} = 12.5 \text{ s}^{-1}$$

If we take down as positive, with respect to the equilibrium position, the ball will start at maximum

displacement, so the position as a function of time is

$$x = A \cos(\omega t) = (0.0500 \text{ m}) \cos [(12.5 \text{ s}^{-1})t]$$

Because the charge is negative, the electric field at the table will be up and the distance from the table is

$$r = H - x = 0.150 \text{ m} - (0.0500 \text{ m}) \cos [(12.5 \text{ s}^{-1})t]$$

The electric field is

$$E = kQ/r^2 = (9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(3.00 \times 10^{-6} \text{ C}) / (0.150 \text{ m} - (0.0500 \text{ m}) \cos [(12.5 \text{ s}^{-1})t])^2$$

$$= (1.08 \times 10^7 \text{ N/C}) / \{3 - \cos [(12.5 \text{ s}^{-1})t]\}^2 \text{ up.}$$

53. We consider the forces on one ball. (The other will be the same except for the reversal.) The separation of the charges is

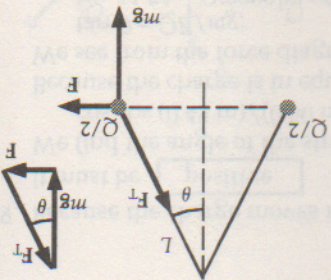
$$r = 2L \sin 30^\circ = 2(0.70 \text{ m}) \sin 30^\circ = 0.70 \text{ m}$$

From the equilibrium force diagram, we have

$$\tan \theta = F/mg = [k(\frac{1}{2}Q)(\frac{1}{2}Q)/r^2] / mg$$

$$\tan 30^\circ = \frac{1}{4}(9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)Q^2 / (0.70 \text{ m})^2 (24 \times 10^{-3} \text{ kg})(9.80 \text{ m/s}^2),$$

$$\text{which gives } Q = 5.4 \times 10^{-6} \text{ C} = 5.4 \mu\text{C}.$$



54. The pea will discharge when the electric field at the surface exceeds the breakdown field. Because we can

treat the charge on the pea as a point charge at the center, we have

$$E = kQ/r^2;$$

$$3 \times 10^6 \text{ N/C} = (9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)Q / (0.375 \times 10^{-2} \text{ m})^2, \text{ which gives } Q = 5 \times 10^{-9} \text{ C}.$$

55. We find the electric field at the location of Q_1 due to the plates and Q_2 .

$$E_2 = kQ_2/x^2$$

$$= (9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(1.3 \times 10^{-6} \text{ C}) / (0.34 \text{ m})^2$$

$$= 1.01 \times 10^5 \text{ N/C (left).}$$

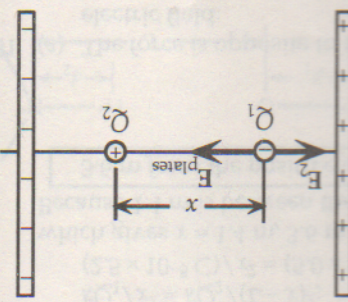
The field from the plates is to the right, so we have

$$E_{\text{net}} = E_{\text{plates}} - E_2$$

$$= 73,000 \text{ N/C} - 1.01 \times 10^5 \text{ N/C} = -2.8 \times 10^5 \text{ N/C (left).}$$

For the force on Q_1 , we have

$$F_1 = Q_1 E_{\text{net}} = (-6.7 \times 10^{-5} \text{ C})(-2.8 \times 10^5 \text{ N/C}) = +0.19 \text{ N (right).}$$



56. We take up as the positive direction and assume that E is up.

From the equilibrium force diagram, we have

$$F_T + QE = mg;$$

$$5.67 \text{ N} + (0.340 \times 10^{-6} \text{ C})E = (0.210 \text{ kg})(9.80 \text{ m/s}^2),$$

$$\text{which gives } E = -1.06 \times 10^7 \text{ N/C (down).}$$

