

33. (a) The directions of the individual fields are shown in the figure. We find the magnitudes of the individual fields:

$$E_1 = E_2 = kQ/L^2.$$

For the components of the resultant field we have

$$E_x = -E_2 \sin 60^\circ = -0.866kQ/L^2;$$

$$E_y = -E_1 - E_2 \cos 60^\circ = -kQ/L^2 - 0.500kQ/L^2 = -1.50kQ/L^2.$$

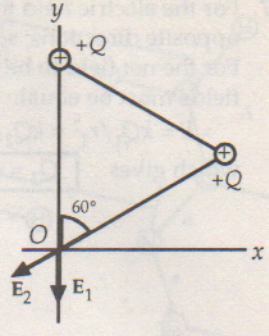
We find the direction from

$$\tan \theta = E_y/E_x = (-1.50kQ/L^2)/(-0.866kQ/L^2) = 1.73, \text{ or } \theta = 60^\circ.$$

We find the magnitude from

$$E = E_x/\cos \theta = (0.866kQ/L^2)/\cos 60^\circ = 1.73kQ/L^2.$$

Thus the field is $1.73kQ/L^2$ 60° below the $-x$ -axis.



(b) The directions of the individual fields are shown in the figure. The magnitudes of the individual fields will be the same:

$$E_1 = E_2 = kQ/L^2.$$

For the components of the resultant field we have

$$E_x = +E_2 \sin 60^\circ = +0.866kQ/L^2;$$

$$E_y = -E_1 + E_2 \cos 60^\circ = -kQ/L^2 + 0.500kQ/L^2 = -0.500kQ/L^2.$$

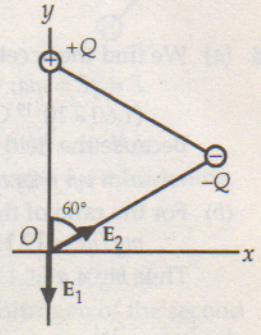
We find the direction from

$$\tan \theta = E_y/E_x = (-0.500kQ/L^2)/(+0.866kQ/L^2) = -0.577, \text{ or } \theta = -30^\circ.$$

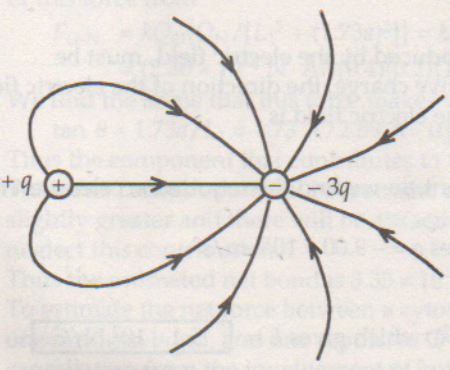
We find the magnitude from

$$E = E_x/\cos \theta = (0.866kQ/L^2)/\cos 30^\circ = kQ/L^2.$$

Thus the field is kQ/L^2 30° below the $+x$ -axis.



34.



35. The acceleration is produced by the force from the electric field:

$$F = qE = ma;$$

$$(1.60 \times 10^{-19} \text{ C})E = (1.67 \times 10^{-27} \text{ kg})(1 \times 10^6)(9.80 \text{ m/s}^2), \text{ which gives } E = \boxed{0.10 \text{ N/C}}$$

36. If we let x be the distance from the center of the Earth, we have

$$GM_{\text{Moon}}/(D-x)^2 = GM_{\text{Earth}}/x^2 = 81GM_{\text{Moon}}/x^2, \text{ or } 81(D-x)^2 = x^2.$$

When we take the square root of both sides, we get

$$x = 9D/10 = 9(3.80 \times 10^5 \text{ km})/10 = \boxed{3.42 \times 10^5 \text{ km from the center of the Earth.}}$$

Note that taking a negative square root gives $x = 9D/8$, the point on the other side of the Moon where the magnitudes are equal, but the fields have the same direction.